New York State Regents Examination in Integrated Algebra

2014 Field Test Analysis, Equating Procedure, and Scaling of Operational Test Forms

Technical Report

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Section I: Introduction

PURPOSE

The purpose of this report is to document the psychometric properties of the New York State Regents Examination in Integrated Algebra. In addition, this report documents the procedures used to analyze the results of the field test and to equate and scale the operational test forms.

Section II: Field Test Analysis

In May 2014, prospective items for the New York State Regents Examination in Integrated Algebra were field tested. The results of this testing were used to evaluate item quality. Only items with acceptable statistical characteristics can be selected for use on operational tests.

Representative student samples for participation in this testing were selected to mirror the demographics of the student population that is expected to take the operational test. The Need/Resource Capacity Categories in Table 1 were used as variables in the sampling plan.

Table 1. Need/Resource Capacity Category Definitions

Need/Resource Capacity (N/RC) Category	Definition
High N/RC Districts: New York City	New York City
Large Cities	Buffalo, Rochester, Syracuse, Yonkers
Urban/Suburban	All districts at or above the 70th percentile on the index with at least 100 students per square mile or enrollment greater than 2500
Rural	All districts at or above the 70th percentile on the index with fewer than 50 students per square mile or enrollment of fewer than 2500
Average N/RC Districts	All districts between the 20th and 70th percentiles on the index
Low N/RC Districts	All districts below the 20th percentile on the index
Charter Schools	Each charter school is a district

FILE PROCESSING AND DATA CLEANUP

The Regents examinations utilize both multiple-choice (MC) and constructed-response (CR) item types in order to more fully assess student ability. Multiple field test (FT) forms were given during this administration to allow for a large number of items to be field tested without placing an undue burden on the students participating in the field test; each student only took a small subset of the items being field tested. The New York State Education Department (NYSED) handled all scanning of the MC responses. Scoring of the CR responses was performed by Measurement Incorporated (MI) under contract with the NYSED. The NYSED and MI produced separate data files, which were provided to Pearson. A test map file that documented the items on each of the FT forms was also provided to Pearson by the NYSED. Finally, student data file layouts containing the position of every field within the student data files from both the NYSED and MI were also provided to Pearson by the NYSED. Upon receipt of these files, Pearson staff checked the data, test map, and layouts for consistency. Any anomalies were referred back to the NYSED for resolution. After these had been resolved and corrected as necessary, final processing of the data file took place. Merging of the NYSED- and MI-provided data was accomplished through uniquely assigned booklet numbers. This processing included the identification and deletion of invalid student test records through the application of a set of predefined exclusion rules[1]. The original student data file received from the NYSED contained 33,308 records (which contained student records for both the Common Core and Non-Common Core portions of the examination); the final field test data file for the Non-Common Core portion contained 10,124 records.

Within the final data file used in the field test analyses, MC responses were scored according to the item keys contained in the test map; correct responses received a score of 1 while incorrect responses received a score of 0. CR item scores were taken directly from the student data file, with the exception that out-of-range scores were assigned scores of 0. For Item Response Theory (IRT) calibrations, blanks (i.e., missing data; not omits) were also scored as 0.

In addition to the scored data, the final data file also contained the unscored student responses and scores. Unscored data were used to calculate the percentage of students who selected the various answer choices for the MC items or the percentage of students who received each achievable score point for the CR items. The frequency of students leaving items blank was also calculated. The scored data were used for all other analyses.

[1] These exclusion rules flagged records without both an MC and a CR component, records with invalid or out-of-range form numbers, records without any responses, and duplicate records. These records were dropped prior to analysis.

CLASSICAL ANALYSIS

Classical Test Theory assumes that any observed test score *x* is composed of both true score *t* and error score *e*. This assumption is expressed as follows:

$$x = t + e$$

All test scores are composed of both a true and an error component. For example, the choice of test items or administration conditions might influence student responses, making a student's observed score higher or lower than the student's true ability would warrant. This error component is random and uncorrelated with (i.e., unrelated to) the student's true score. Across an infinitely large number of administrations, the mean of the error scores would be zero. Thus, the best estimate of a student's true score for any test administration (or their expected score given their [unobservable] true level of ability or true score) is that student's observed score. This expectation is expressed as follows:

$$E(x) = t$$

Item difficulties, point-biserial correlations, reliability estimates, and various statistics related to rater agreement have been calculated and are summarized in the following section.

Item Difficulty

Item difficulty is typically defined as the average of scores for a given item. For MC items, this value (commonly referred to as a p-value) ranges from 0 to 1. For CR items, this value ranges from 0 to the maximum possible score. In order to place all item means on a common metric (ranging from 0 to 1), CR item means were divided by the maximum points possible for the item.

Item Discrimination

Item discrimination is defined as the correlation between a score on a given test question and the overall raw test score. These correlations are Pearson correlation coefficients. For MC items, it is also known as the point-biserial correlation.

Table 2 presents a summary of the classical item analysis for each of the field test forms. The first three columns from the left identify the form number, the number of students who took each form, and the number of items on each field test form, respectively. The remaining columns are divided into two sections (i.e., item difficulty and discrimination). Recall that for CR items, item means were divided by the maximum number of points possible in order to place them in the same metric as the MC items. There were no items with difficulties that were greater than 0.90 and 4 items had correlations that were less than 0.25. In addition to the summary information provided in Table 2, further classical item statistics are provided in Appendix A.

Table 2. Classical Item Analysis Summary

Form	N-Count	No. of Items	Item Difficulty			Item Discrimination		
			<0.50	0.50 to 0.90	>0.90	<0.25	0.25 to 0.50	>0.50
141	598	11	5	6	0	0	6	5
142	597	11	9	2	0	0	7	4
143	601	11	9	2	0	0	6	5
144	594	11	7	4	0	0	6	5
145	594	11	8	3	0	1	7	3
146	612	11	9	2	0	0	8	3
147	612	11	6	5	0	0	8	3
148	618	11	10	1	0	0	8	3
149	601	11	10	1	0	0	5	6
150	605	11	9	2	0	0	8	3
151	593	11	9	2	0	1	4	6
152	596	11	7	4	0	0	6	5
153	584	11	8	3	0	0	8	3
154	579	11	9	1	0	1	7	2
155	589	11	8	3	0	0	8	3
156	576	11	8	3	0	1	5	5
157	575	11	8	3	0	0	6	5

For some forms, the item counts in the “Item Difficulty” and “Item Discrimination” columns may not sum to the value in the “No. of Items” column due to DNS (Do Not Score) items.

Test Reliability

Reliability is the consistency of the results obtained from a measurement with respect to time or between items or subjects that constitute a test. As such, test reliability can be estimated in a variety of ways. Internal consistency indices are a measure of how consistently examinees respond to items within a test. Two factors influence estimates of internal consistency: (1) test length and (2) homogeneity of the items. In general, the more items on the examination, the higher the reliability and the more similar the items, the higher the reliability.

Table 3 contains the internal consistency statistics for each of the field test forms under the heading “Test Reliability.” These statistics ranged from 0.53 to 0.72. It should be noted that these field test forms are very short (11 items); operational tests generally are composed of more items and would be expected to have higher reliabilities than do these field test forms.

Scoring Reliability

One concern with CR items is the reliability of the scoring process (i.e., consistency of the score assignment). CR items must be read by scorers who assign scores based on a comparison between the rubric and student responses. Consistency between

scorers is a critical part of the reliability of the assessment. To track scorer consistency, approximately 10% of the test booklets are scored a second time (these are termed "second read scores") and compared to the original set of scores (also known as "first read scores").

As an overall measure of scoring reliability, the Pearson correlation coefficient between the first and second scores for all CR items with second read scores was computed for each form. This statistic is often used as an overall indicator of scoring reliability, and it generally ranges from 0 to 1. Table 3 contains these values in the column headed "Scoring Reliability." They ranged from 0.88 to 0.96, indicating a fair to high degree of reliability across the forms.

Table 3. Test and Scoring Reliability

Form Number	Test Reliability	Scoring Reliability
141	0.70	0.93
142	0.62	0.94
143	0.68	0.88
144	0.68	0.90
145	0.62	0.90
146	0.68	0.93
147	0.63	0.90
148	0.63	0.94
149	0.69	0.89
150	0.62	0.89
151	0.72	0.95
152	0.69	0.89
153	0.65	0.96
154	0.53	0.89
155	0.68	0.94
156	0.68	0.95
157	0.67	0.95

Interrater Agreement

For each CR item, the difference between the first and second reads was tracked and the number of times each possible difference between the scores occurred was tabulated. These values were then used to calculate the percentage of times each possible difference occurred. When examining interrater agreement statistics, it should be kept in mind that the maximum number of points per item varies, as shown in the "Score Points" column. Blank cells in the table indicate out-of-range differences (e.g., It is impossible for two raters to differ by more than one point in their scores on an item with a maximum possible score of one; cells in the table other than −1, 0, and 1 would therefore be blanked out.).

Appendix B contains the proportion of occurrence of these differences for each CR item. CR item maximum point values ranged between two and four. Rates of exact agreement (i.e., differences of zero points) ranged between 62% and 97%. Appendix C contains additional summary information regarding the first and second reads, including the percentage of first and second scores that were exact or adjacent matches. Percentages of exact or adjacent agreement ranged between 91% and 100%.

Constructed-Response Item Means and Standard Deviations

Appendix C also contains the mean and standard deviation of the first and second scores for each CR item. The largest difference between the item means for the first and second read scores was 0.1, while the largest difference between the standard deviations was 0.09.

Intraclass Correlation

In addition, Appendix C contains the intraclass correlations for the items. These correlations are calculated using a formulation given by Shrout and Fleiss (1979). Specifically, they described six different models based on various configurations of judges and targets (in this case, papers that are being scored). For this assessment, the purpose of the statistic is to describe the reliability of single ratings, and each paper is scored by two judges who are randomly assigned from the larger pool of judges, and who score multiple papers. This description fits their "Case 1." Further, they distinguish between situations where the score assigned to the paper is that of a single rater versus that where the score is the mean of k raters. Since the students' operational scores are those from single (i.e., the first) raters, the proper intraclass correlation in this instance is termed by Shrout and Fleiss as "ICC(1,1)." It will be referred to herein simply as the "intraclass correlation" (ICC).

While the ICC is a bona fide correlation coefficient, it differs from a regular correlation coefficient in that its value remains the same, regardless of how the raters are ordered. A regular Pearson correlation coefficient would change values if, for example, half of the second raters were switched to the first position, while the ICC would maintain a consistent value. Because the papers were randomly assigned to the judges, ordering is arbitrary, and thus the ICC is a more appropriate measure of reliability than the Pearson correlation coefficient in this situation. The ICC ranges from zero (the scores given by the two judges are unrelated) to one (the scores from the two judges match perfectly); negative values are possible, but rare, and have essentially the same meaning as values of zero. It should also be noted that the ICC can be affected by low degrees of variance in the scores being related, similar to the way that regular Pearson correlation coefficients are affected. ICCs for items where almost every examinee achieved the same score point (e.g., an extremely easy dichotomous item where almost every examinee was able to answer it correctly) may have a low or negative ICC, even though almost all ratings by the judges matched exactly.

McGraw and Wong (1996, Table 4, p. 35) state that the ICC can be interpreted as "the degree of absolute agreement among measurements made on randomly selected objects. It estimates the correlation of any two measurements." Since it is a correlation

coefficient, its square indicates the percent of variance in the scores that is accounted for by the relationship between the two sets of scores (i.e., the two measurements). In this case, these scores are those of the pair of judges. ICC values greater than 0.60 indicate that at least 36% (0.60^2) of the variation in the scores given by the raters is accounted for by variations in the responses to the items that are being scored (e.g., variations in the ability being measured) rather than by variations caused by a combination of differences in the severity of the judges, interactions between judge severity and the items, and random error (e.g., variations exterior to the ability being measured). It is generally preferred that items have ICCs at this level or higher. Only one item had ICCs below 0.60. Consistent with other information provided in the table, these values indicate a high to very high level of scoring reliability for almost all of the items in the field test.

Weighted Kappa

Weighted Kappa (Cohen, 1968) was also calculated for each item, based on the first and second reads and is included in Appendix C as well. This statistic is an estimate of the agreement of the score classifications over and above that which would be expected to occur by chance. Similar to the ICC, its value can range between zero (the scores given by the judges agree as often as would be expected by chance) and one (scores given by the judges agree perfectly). In addition, negative values are possible, but rare, and have the same interpretation as zero values. One set of guidelines for the evaluation of this statistic is (Fleiss, 1981):

- $k > 0.75$ denotes excellent reproducibility
- $0.4 < k \leq 0.75$ denotes good reproducibility
- $0 < k \leq 0.4$ denotes marginal reproducibility

The results show excellent reproducibility between the first and second reads for all but eight items, and good reproducibility for all of those eight. No item displayed marginal reproducibility. The scoring reliability analyses offer strong evidence that the scoring of the CR items was performed in a reliable to a highly reliable manner.

ITEM RESPONSE THEORY (IRT) AND THE CALIBRATION AND EQUATING OF THE FIELD TEST ITEMS

While classical test theory-based statistical measures are useful for assessing the suitability of items for operational use (i.e., use as part of an assessment used to measure student ability and thus having real-world consequences for students, teachers, schools, and administrators), their values are dependent on both the psychometric properties of the items and the ability distributions of the samples upon which they are based. In other words, classical test theory-based statistics are *sample-dependent statistics*.

In contrast, Item Response Theory (IRT)-based statistics are not dependent on the sample over which they are estimated—they are invariant across different samples (Hambleton, Swaminathan & Rogers, 1991; Lord, 1980). This invariance allows student

ability to be estimated on a common metric even if different sets of items are used (as with different test forms over different test administrations).

The process of estimating IRT-based item parameters is referred to as "item calibration," and the placing of these parameters on a common metric or scale is termed "equating." While one reason for the field testing of items is to allow their suitability for use in the operational measurement of student ability to be assessed, the data resulting from field testing is also used to place items on the scale of the operational test (i.e., they are equated to the operational metric). Once items are on this common metric, any form composed of items from this pool can be scaled (the process through which scale score equivalents for each achievable raw score are derived) and the resulting scale scores will be directly comparable to those from other administrations, even though the underlying test forms are composed of different sets of items.

There are several variations of IRT that differ mainly in the way item behavior is modeled. The New York State Regents Examinations use the Rasch family of IRT statistics (Rasch, 1980; Masters, 1982) to calibrate, scale, and equate all subjects.

The most basic expression of the Rasch model is in the item characteristic curve. It conceptualizes the probability of a correct response to an item as a function of the ability level and the item's difficulty. The probability of a correct response is bounded by "1" (certainty of a correct response) and "0" (certainty of an incorrect response). The ability scale is theoretically unbounded. In practice, the ability scale ranges from approximately −4 to +4 logits. The relationship between examinee ability θ, item difficulty D_i, and probability of answering the item correctly P_i is shown in the equation below:

$$P_i(\theta) = \frac{\exp\,(\theta - D_i)}{1 + \exp\,(\theta - D_i)}$$

Examinee ability (θ) and item difficulty (D_i) are on the same scale. This is useful for certain purposes. An examinee with an ability level equal to the item difficulty will have a 50% chance of answering the item correctly; if his or her ability level is higher than the item difficulty, then the probability of answering the item correctly is commensurately higher, and the converse is also true.

The Rasch Partial Credit Model (PCM) (Masters, 1982) is a direct extension of the dichotomous one-parameter IRT model above. For an item involving m score categories, the general expression for the probability of achieving a score of x on the item is given by

$$P_x(\theta) = \frac{\exp[\sum_{k=0}^{x}(\theta - D_k)]}{\sum_{h=0}^{m}\exp[\sum_{k=0}^{h}(\theta - D_k)]}$$

where

$$D_0 \equiv 0.0$$

In the above equation, P_x is the probability of achieving a score of x given an ability of θ; m is the number of achievable score points minus one (note that the subscript k runs from 0 to m); and D_k is the step parameter for step k. The steps are numbered from 0 to the number of achievable score points minus one, and step 0 (D_0) is defined as being equal to zero. Note that a four-point item, for example, usually has five achievable score points (0, 1, 2, 3, and 4), thus the step numbers usually mirror the achievable point values.

According to this model, the probability of an examinee scoring in a particular category (step) is the sum of the logit (log-odds) differences between θ and D_k of all the completed steps, divided by the sum of the differences of all the steps of an item. Thissen and Steinberg (1986) refer to this model as a divide-by-total model. The parameters estimated by this model are m_{i-1} threshold (difficulty) estimates and represent the points on the ability continuum where the probability of the examinee achieving score m_i exceeds that of m_{i-1}. The mean of these threshold estimates is used as an overall summary of the polytomous item's difficulty.

If the number of achievable score points is one (i.e., the item is dichotomous), then the PCM reduces to the basic Rasch IRT model for dichotomous items. This means that dichotomous and polytomous items are being scaled using a common model and therefore can be calibrated, equated, and scaled together. It should be noted that the Rasch model assumes that all items have equal levels of discrimination and that there is no guessing on MC items. However, it is robust to violations of these assumptions, and items that violate these assumptions to a large degree are usually flagged for item-model misfit.

Item Calibration

When interpreting IRT item parameters, it is important to remember that they do not have an absolute scale—rather, their scale (in terms of mean and standard deviation) is purely arbitrary. It is conventional to set the mean of the item difficulties to zero when an assessment is scaled for the first time. Rasch IRT scales the theta measures in terms of *logits*, or "log-odds units." The length of a logit varies from test to test, but generally, the standard deviation of the item difficulties of a test scaled for the first time will be somewhere in the area of 0.6–0.8. While the item difficulties are invariant with respect to one another, the absolute level of difficulty represented by their mean is dependent on the overall difficulty of the group of items with which it was tested. In addition, there is no basis for assuming that the difficulty values are normally distributed around their mean—their distribution again depends solely upon the intrinsic difficulties of the items themselves. Thus, if a particularly difficult set of items (relative to the set of items originally calibrated) was field tested, their overall mean would most probably be greater than zero, and their standard deviation would be considerably less than one. In addition, they would most probably not be normally distributed.

Rasch item difficulties generally range from −3.0 to 3.0, although very easy or difficult items can fall outside of this range. Items should not be discounted solely on the basis of their difficulty. A particular topic may require either a difficult or an easy item. Items are usually most useful if their difficulty is close to a cut score, as items provide the highest level of information at the ability level equal to their difficulty. Items with difficulties farther away from the cuts provide less information about students with abilities close to the cut scores (and, hence, are more susceptible to misclassification), but are still useful. In general, items should be selected for use based on their content, with their Rasch difficulty being only a secondary consideration.

Item Fit Evaluation

The INFIT statistic is used to assess how well items fit the Rasch model. Rasch theory models the probability of a student being able to answer an item correctly as a function of the student's level of ability and the item's difficulty, as stated previously. The Rasch model also assumes that items' discriminations do not differ, and that the items are not susceptible to guessing. If these assumptions do not hold (if, for example, an item has an extremely high or low level of discrimination), then the item's behavior will not be well modeled by Rasch IRT. Guidelines for interpretation of the INFIT statistic are taken from Linacre (2005), and can be found in Table 4 below.

Table 4. Criteria to Evaluate Mean-Square Fit Statistics

INFIT	Interpretation
>2.0	Distorts or degrades the measurement system
1.5–2.0	Unproductive for construction of measurement, but not degrading
0.5–1.5	Productive for measurement
< 0.5	Unproductive for measurement, but not degrading. May produce misleadingly good reliabilities and separations

INFIT is an information-weighted fit statistic, which is more sensitive to unexpected behavior affecting responses to items near the person's measure (or ability) level. In general, values near 1.0 indicate little distortion of the measurement system, while values less than 1.0 indicate observations that are too predictable (redundancy, model overfit). Values greater than 1.0 indicate unpredictability (unmodeled noise, model underfit).

Table 5 contains a summary of the analysis for each of the field test forms. The first column from the left lists the form numbers. The next two columns list the number of students who participated and the number of items on each field test form, respectively. The following columns show the frequency of items at three levels of difficulty (easier items with a Rasch difficulty <−2.0, moderate items with a Rasch difficulty between −2.0 and 2.0, and more difficult items with a Rasch difficulty >2.0), and frequencies of item misfits as classified in the preceding table. All items except one fell within the moderate −2.0 to +2.0 difficulty range, and there were no items with an INFIT statistic outside the range most productive for measurement. Item level results of the analysis can be found in Appendix D.

Table 5. Partial-Credit Model Item Analysis Summary

Form	N-Count	No. of Items	Rasch			INFIT			
			<−2.0	−2.0 to 2.0	>2.0	<0.5	0.5 to 1.5	1.5 to 2.0	>2.0
141	598	11	0	11	0	0	11	0	0
142	597	11	0	11	0	0	11	0	0
143	601	11	0	11	0	0	11	0	0
144	594	11	0	11	0	0	11	0	0
145	594	11	1	10	0	0	11	0	0
146	612	11	0	11	0	0	11	0	0
147	612	11	0	11	0	0	11	0	0
148	618	11	0	11	0	0	11	0	0
149	601	11	0	11	0	0	11	0	0
150	605	11	0	11	0	0	11	0	0
151	593	11	0	11	0	0	11	0	0
152	596	11	0	11	0	0	11	0	0
153	584	11	0	11	0	0	11	0	0
154	579	11	0	10	0	0	10	0	0
155	589	11	0	11	0	0	11	0	0
156	576	11	0	11	0	0	11	0	0
157	575	11	0	10	1	0	11	0	0

For some forms, the item counts in the “Rasch” and “INFIT” columns may not sum to the value in the “No. of Items” column due to DNS (Do Not Score) items.

DIFFERENTIAL ITEM FUNCTIONING

Differential Item Functioning (DIF) occurs when members of a particular group have a different probability of success than members of another group who have the same level of ability for reasons unrelated to the academic skill or construct being measured. For example, items testing English grammar skills may be more difficult for LEP students as opposed to non-LEP students, but such differences are likely due to the fact that the item measures an academic skill related to English language proficiency. Such items would not be considered to be functioning differentially.

The Mantel Chi-Square and Standardized Mean Difference

The Mantel χ^2 is a conditional mean comparison of the ordered response categories for reference and focal groups combined over values of the matching variable score. “Ordered” means that a response earning a score of “1” on an item is better than a response earning a score of “0” or “2” is better than “1,” and so on. “Conditional,” on the other hand, refers to the comparison of members from the two groups who received the same score on the matching variable, that is, the total test score in our analysis.

Group	Item Score				Total
	y_1	y_2	…	y_T	
Reference	n_{R1k}	n_{R2k}	…	n_{Rtk}	n_{R+k}
Focal	n_{F1k}	n_{F2k}	…	n_{Ftk}	n_{F+k}
Total	n_{+1k}	n_{+2k}	…	n_{+tk}	n_{++k}

Figure 1. 2 × *t* Contingency Table at the kth of K Levels.

Figure 1 (from Zwick, Donoghue & Grima, 1993) shows a 2 × *t* contingency table at the k^{th} of *K* levels, where *t* represents the number of response categories and *k* represents the number of levels of the matching variable. The values $y_1, y_2, \ldots y_T$ represent the *t* scores that can be gained on the item. The values n_{Ftk} and n_{Rtk} represent the numbers of focal and reference groups who are at the k^{th} level of the matching variable and gain an item score of y_t. The "+" indicates the total number over a particular index (Zwick et al., 1993). The Mantel statistic is defined as the following formula:

$$Mantel\chi^2 = \frac{\left(\sum_k F_k - \sum_k E(F_k)\right)^2}{\sum_k Var(F_k)}$$

in which F_k represents the sum of scores for the focal group at the k^{th} level of the matching variable and is defined as follows:

$$F_k = \sum_t y_t n_{Ftk}$$

The expectation of F_k under the null hypothesis is

$$E(F_k) = \frac{n_{F+k}}{n_{++k}} \sum_t y_t n_{Ftk}$$

The variance of F_k under the null hypothesis is as follows:

$$Var(F_k) = \frac{n_{R+k} n_{F+k}}{n_{++k}^2 (n_{++k} - 1)} \left[(n_{++k} \sum_t y_t^2 n_{+tk}) - (\sum_t y_t n_{+tk})^2 \right]$$

Under *H0*, the Mantel statistic has a chi-square distribution with one degree of freedom. In DIF applications, rejecting *H0* suggests that the students of the reference and focal groups who are similar in overall test performance tend to differ in their mean performance on the item. For dichotomous items, the statistic is identical to the Mantel-Haenszel (MH) (1959) statistic without the continuity correction (Zwick et al., 1993).

A summary statistic to accompany the Mantel approach is the standardized mean difference (SMD) between the reference and focal groups proposed by Dorans and Schmitt (1991). This statistic compares the means of the reference and focal groups, adjusting for differences in the distribution of the reference and focal group members across the values of the matching variable. The SMD has the following form:

$$SMD = \sum_k p_{Fk} m_{Fk} - \sum_k p_{Fk} m_{Rk}$$

in which

$$p_{Fk} = \frac{n_{F+k}}{n_{F++}}$$

is the proportion of the focal group members who are at the k^{th} level of the matching variable;

$$m_{Fk} = \frac{1}{n_{F+k}\sum_{t} y_t n_{Ftk}}$$

is the mean item score of the focal group members at the k^{th} level; and m_{Rk} is the analogous value for the reference group. As can be seen from the equation above, the SMD is the difference between the unweighted item mean of the focal group and the weighted item mean of the reference group. The weights for the reference group are applied to make the weighted number of the reference-group students the same as in the focal group within the same level of ability. A negative SMD value implies that the focal group has a lower mean item score than the reference group, conditional on the matching variable.

Multiple-Choice Items

For the MC items, the MH odds ratio (converted to the ETS delta scale [D]) is used to classify items into one of three categories of DIF.

The Odds Ratio

The odds of a correct response (proportion passing divided by proportion failing) are *P/Q* or *P/(1−P)*. The *odds ratio* is the odds of a correct response of the reference group divided by the odds of a correct response of the focal group. For a given item, the odds ratio is defined as follows:

$$\alpha_{MH} = \frac{P_r/Q_r}{P_f/Q_f}$$

and the corresponding null hypothesis is that the odds of getting the item correct are equal for the two groups. Thus, the odds ratio is equal to 1:

$$\alpha_{MH} = \frac{P_r/Q_r}{P_f/Q_f} = 1$$

The Delta Scale

To make the odds ratio symmetrical around zero with its range being in the interval −∞ to +∞, the odds ratio is transformed into a log-odds ratio according to this equation:

$$\beta_{MH} = \ln(\alpha_{MH})$$

This simple, natural logarithm transformation of the odds ratio is symmetrical around zero. This DIF measure is a signed index; a positive value signifies DIF in favor of the

reference group, a negative value indicates DIF in favor of the focal group, and zero has the interpretation of equal odds of success on the item. β_{MH} also has the advantage of a linear relationship to other interval scale metrics (Camilli & Shepard, 1994). β_{MH} is placed on the ETS delta scale (D) using the following equation:

$$D = -2.35\beta_{MH}$$

DIF Classification for MC Items

Table 6 depicts DIF classifications for MC items. Classification depends on the delta (D) value and the significance of its difference from zero ($p < 0.05$). The criteria are derived from those used by the National Assessment of Educational Progress (Allen, Carlson, & Zelenak 1999) in the development of their assessments.

Table 6. DIF Classification for MC Items

Category	Description	Criterion
A	No DIF	D not significantly different from zero or $\|D\| < 1.0$
B	Moderate DIF	$1.0 \leq \|D\| < 1.5$ or not otherwise A or C
C	High DIF	D is significantly different from zero and $\|D\| \geq 1.5$

DIF Classification for CR Items

The SMD is divided by the total group item standard deviation to obtain an effect-size value for the SMD (ES_{SMD}). The value of ES_{SMD} and the significance of the Mantel χ^2 statistic ($p < 0.05$) are then used to determine the DIF category of the item as depicted in Table 7 below.

Table 7. DIF Classification for CR Items

Category	Description	Criterion
AA	No DIF	Non-significant Mantel χ^2 or $\|ES_{SMD}\| \leq 0.17$
BB	Moderate DIF	Significant Mantel χ^2 and $0.17 < \|ES_{SMD}\| \leq 0.25$
CC	High DIF	Significant Mantel χ^2 and $0.25 < \|ES_{SMD}\|$

Reliable DIF results are dependent on the number of examinees in both the focal and reference groups. Clauser and Mazor (1998) state that a minimum of 200 to 250 examinees per group is sufficient to provide reliable results. Some testing organizations require as many as 300 to 400 examinees per group (Zwick, 2012) in some applications. For the field testing of the Regents examinations, the sample sizes were such that only comparisons based on gender (males vs. females) were possible. Even for gender, sample sizes were only moderately large, and so the results should be interpreted with caution.

The DIF statistics for gender are shown in Appendix E. MC items in DIF categories “B” and “C” and CR items in categories “BB” and “CC” were flagged. These flags are shown in the “DIF Category” column (“A” and “AA” category items will have blank cells here). The “Favored Group” column indicates which gender is favored for items that are flagged.

Section III: Equating Procedure

Students particpating in the 2014 field test administration for the New York State Regents Examination in Integrated Algebra received one of 57 test forms (numbered 101–157). Forms 141–157 addressed the Non-Common Core based curriculum. Forms 146 and 147 were the anchor forms for the equating, and were intact forms that had been administered in the prior year. Because the forms had been previously administered, their items had known parameters on the operational scale. The remaining test forms were composed of items that had not been administered to New York State students. Test forms were spiraled within classrooms, so that students had an equal chance of receiving any of the 57 forms, depending solely on their ordinal position within the classroom. In essence, students were randomly assigned to test forms, forming randomly equivalent groups taking each of the forms. Appendices A and D (with the classical and Rasch IRT item level statistics) may be consulted to determine the characteristics of the items (e.g., item type and maximum number of points possible) that made up each form.

RANDOMLY EQUIVALENT GROUP EQUATING DESIGN

The equating analyses were based on the assumption that the groups taking the different forms had equivalent ability distributions and means. Given the random assignment of forms to examinees, this was a reasonable assumption. The initial step in the analyses was to calibrate all forms, both the anchor form and the remaining field test forms. All forms were calibrated using Winsteps, version 3.60 (Linacre, 2005).

The anchor form calibration began with all anchor item difficulty parameters fixed to their known values from the previous year. Because it is possible for item parameters to "drift" (shift their difficulties relative to one another), a stability check was integrated into the analysis.

Winsteps provides an item level statistic, termed "displacement." Linacre (2011, p. 545) describes this statistic as:

> …the size of the change in the parameter estimate that would be observed in the next estimation iteration if this parameter was free (unanchored) and all other parameter estimates were anchored at their current values. For a parameter (item or person) that is anchored in the main estimation, (the displacement value) indicates the size of disagreement between an estimate based on the current data and the anchor value.

This statistic was used to identify items with difficulties that had shifted, relative to the difficulties of the other items on the form. After the intial calibration run, the Winsteps displacement values for all anchor form items were examined for absolute values greater than 0.30. If present, the item with the largest absolute displacement value was removed from anchored status but remained on the test form. Its difficulty value was subsequently reestimated relative to the difficulties of the remaining anchored items. The Winsteps calibration was then rerun with the reduced anchor set, after which the

displacement values were again checked for absolute values in excess of 0.30. If another was found, it was also removed from anchored status and the calibration rerun. This iterative procedure continued until all anchored items had displacements of 0.30 or less. Five items were identified as having drifted for the 2014 analyses, one in Form 146 and 4 in Form 147.

After a stable anchor item set had been identified, the mean of the ability estimates of the students who took the anchor forms were computed[2]. The average of these mean ability estimates was then used as the target ability for the forms with the field test items. Because the groups taking the different forms were randomly equivalent and thus had the same mean ability, adjustment of the parameters of the field test items on any form to values that produced an ability distribution for students who had taken the form with a mean equal to a common target ability from the anchor forms would result in the parameters for the field test items on that form being equated to the scale of the anchor form, which was also the operational scale. Because this target was derived from multiple anchor forms, the anchor forms were also equated to this common target.

The equated mean ability estimate for Form 146 was −0.08 and for Form 147 was −0.59. The average of these means was −0.34. This value became the target for the field test form equating.

The next step was the initial calibration of the field test forms (including the anchor forms). This was a “free” calibration, meaning that the item parameters were not constrained in any way. This initial calibration produced a set of Rasch difficulty parameters for the items on each form. Also produced as a part of the Winsteps calibration was a set of person ability estimates for each form.

The next step was the computation of an equating constant for each form. Under Rasch IRT, if all of the difficulty parameters on a form have a constant added to them, the ability estimates for examinees will also be changed from their previous values by the amount represented by that constant. Therefore, to adjust the item difficulty parameters such that the mean of the ability distribution is set equal to the target mean ability from the anchor form, an equating constant was calculated for each field test form by subtracting the field test form mean ability from the target mean ability. This value was then added to the Rasch difficulty parameter of all items on the field test form. These adjusted values were then used as anchors for a second Winsteps calibration of the field test form. The mean of the person ability values from this second calibration was computed and compared to the target mean. If the anchored field test mean ability differed from the target mean ability by 0.005 or more, then an additional equating constant was computed using the difference between the mean ability from the field test form anchored run and the target mean ability, and another anchored run was completed. This process continued until all adjusted field test form mean abilities were within the 0.005 tolerance limit around the targeted mean ability. The final equating

[2] Because under Rasch IRT the ability of students with extreme scores (either zero or perfect scores) cannot be exactly computed (they are equal to $-\infty$ and $+\infty$, respectively), they were excluded from this and all other analyses for both the anchor and other field test forms.

constant for any field test form was the sum of the constants from each anchored round for that form. At this point, with the adjusted mean abilities for the field test forms all equal (within the specified limits) to the target abilities, all of the adjusted field test item parameters and the anchor item parameters were on the common operational scale, and thus could be used in any subsequent operational administration. The initial mean abilities and final equating constants for the field test forms can be found in Table 8.

Table 8. Initial Mean Abilities and Equating Constants

Form Number	Mean Ability	Constant
141	−0.17	−0.15
142	−0.44	0.11
143	−0.38	0.04
144	−0.45	0.11
145	−0.40	0.06
146	−0.28	−0.06
147	−0.21	−0.10
148	−0.54	0.19
149	−0.70	0.33
150	−0.52	0.19
151	−0.52	0.17
152	−0.41	0.08
153	−0.48	0.14
154	−0.62	0.27
155	−0.60	0.25
156	−0.41	0.07
157	−0.58	0.23

Section IV: Scaling of Operational Test Forms

Operational test items were selected based on content coverage, content accuracy, and statistical quality. The sets of items on each operational test conformed to the coverage determined by content experts working from the learning standards established by the New York State Education Department and explicated in the test blueprint. Each item's classical and Rasch statistics were used to assess item quality. Items were selected to vary in difficulty to accurately measure students' abilities across the ability continuum. Appendix F contains the 2014 operational test maps for the January, June, and August administrations.

All Regents examinations have two cut scores, which are set at the scale scores of 65 and 85. One of the primary considerations during test construction was to select items so as to minimize changes in the raw scores corresponding to these two scale scores. Maintaining a consistent mean Rasch difficulty level from administration to administration facilitates this. For this assessment, the target value for the mean Rasch difficulty was set at 0.083. It should be noted that the raw scores corresponding to the scale score cut scores may still fluctuate even if the mean Rasch difficulty level is maintained at the target value due to differences in the distributions of the Rasch difficulty values amongst the items from administration to administration.

The relationship between raw and scale scores is explicated in the scoring tables for each administration. These tables can be found in Appendix G, and cover the January, June, and August administrations. These tables are the end product of the following scaling procedure.

All Regents examinations are equated back to a base scale that is held constant from year to year. Specifically, they are equated to the base scale through the use of a calibrated item pool. The Rasch difficulties from the item's initial administration in a previous year's field test are used to equate the scale for the current administration to the base administration. For this examination, the base administration was the June 2008 administration. Scale scores from the 2014 administrations are on the same scale, and can be directly compared to scale scores on all previous administrations back to and including the June 2008 administration.

When the base administration was concluded, the initial raw score-to-scale score relationship was established. Four raw scores were fixed at specific scale scores. Scale scores of 0 and 100 were fixed to correspond to the minimum and maximum possible raw scores. In addition, a standard setting had been held to determine the passing and passing with distinction cut scores in the raw score metric. The scale score points of 65 and 85 were set to correspond to those raw score cuts. A third-degree polynomial is required in order to fit a line exactly to four arbitrary points (e.g., the raw scores corresponding to the four critical scale scores of 0, 65, 85, and 100). The general form of this best-fitting line is:

$$SS = m_3*RS^3 + m_2*RS^2 + m_1*RS + m_0$$

where *SS* is the scaled score, *RS* is the raw score, and m_0 through m_3 are the transformation constants that convert the raw score into the scale score (please note that m_0 will always be equal to zero in this application since a raw score of zero corresponds to a scale score of zero). The above relationship and the values of m_1 to m_3 specific to this subject were then used to determine the scale scores corresponding to the remainder of the raw scores on the examination. This initial relationship between the raw and scale scores became the base scale.

The Rasch difficulty parameters for the items on the base form were then used to derive a raw score-to-Rasch student ability (theta score) relationship. This allowed the

relationship between the Rasch theta score and the scale score to be known, mediated through their common relationship with the raw scores.

In succeeding years, each test form was selected from the pool of items that had been tested in previous years' field tests, each of which had known Rasch item difficulty parameter(s). These known parameters were then used to construct the relationship between the raw and Rasch theta scores for that particular form. Because the Rasch difficulty parameters are all on a common scale, the Rasch theta scores were also on a common scale with previously administered forms. The remaining step in the scaling process was to find the scale score equivalent for the Rasch theta score corresponding to each raw score point on the new form using the theta-to-scale score relationship established in the base year. This was done via linear interpolation.

This process results in a relationship between the raw scores on the form and the overall scale scores. The scale scores corresponding to each raw score are then rounded to the nearest integer for reporting on the conversion chart (posted at the close of each administration). The only exceptions are for the minimum and maximum raw scores and the raw scores that correspond to the scaled cut scores of 65 and 85.

The minimum (zero) and maximum possible raw scores are assigned scale scores of 0 and 100, respectively. In the event that there are raw scores less than the maximum with scale scores that round to 100, their scale scores are set equal to 99. A similar process is followed with the minimum score; if any raw scores other than zero have scale scores that round to zero, their scale scores are instead set equal to one.

With regard to the cuts, if two or more scale scores round to either 65 or 85, the lowest raw score's scale score is set equal to a 65 or 85 and the scale scores corresponding to the higher raw scores are set to 66 or 86 as appropriate. If no scale score rounds to either of these two critical cuts, then the raw score with the largest scale score that is less than the cut is set equal to the cut. The overarching principle when two raw scores both round to either scale score cut is that the lower of the raw scores is always assigned to be equal to the cut so that students are never penalized for this ambiguity.

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Appendix A: Classical Item Analysis

In the following table, “Max” is the maximum number of possible points. “N-Count” refers to the number of student records in the analysis. “Alpha” contains Cronbach’s Coefficient α (since this is a test [form] level statistic, it has the same value for all items within each form). For MC items, “B” represents the proportion of students who left the item blank, and “M1” through “M4” are the proportions of students who selected each of the four answer choices. For CR items, “B” represents the proportion of students who left the item blank, and “M0” through “M4” are the proportions of students who received scores of 0 through 4. “Mean” is the average of the scores received by the students. The final (right) column contains the Point-Biserial correlation for each item. There may be some instances of items with missing statistics; this occurs when an item was not scored.

Test	Form	Type	Item	Max	N-Count	Alpha	B	M0	M1	M2	M3	M4	Mean	Point-Biserial
2014_IALG	141	MC	01	1	598	0.70	0.04		0.14	0.66	0.14	0.01	0.66	0.46
2014_IALG	141	MC	02	1	598	0.70	0.06		0.19	0.52	0.13	0.11	0.19	0.43
2014_IALG	141	MC	03	1	598	0.70	0.05		0.61	0.14	0.11	0.08	0.61	0.48
2014_IALG	141	MC	04	1	598	0.70	0.05		0.05	0.31	0.37	0.22	0.31	0.49
2014_IALG	141	MC	05	1	598	0.70	0.06		0.28	0.14	0.36	0.16	0.36	0.32
2014_IALG	141	MC	06	1	598	0.70	0.06		0.10	0.11	0.20	0.54	0.54	0.59
2014_IALG	141	MC	07	1	598	0.70	0.07		0.10	0.27	0.53	0.04	0.53	0.49
2014_IALG	141	MC	08	1	598	0.70	0.07		0.04	0.72	0.04	0.13	0.72	0.51
2014_IALG	141	CR	09	2	598	0.70	0.12	0.25	0.18	0.46			1.09	0.60
2014_IALG	141	CR	10	3	598	0.70	0.17	0.21	0.02	0.46	0.14		1.36	0.64
2014_IALG	141	CR	11	4	598	0.70	0.20	0.52	0.12	0.05	0.02	0.09	0.62	0.65
2014_IALG	142	MC	01	1	597	0.62	0.05		0.13	0.35	0.35	0.12	0.35	0.54
2014_IALG	142	MC	02	1	597	0.62	0.06		0.17	0.20	0.32	0.25	0.25	0.33
2014_IALG	142	MC	03	1	597	0.62	0.05		0.12	0.49	0.24	0.09	0.49	0.44
2014_IALG	142	MC	04	1	597	0.62	0.07		0.40	0.29	0.13	0.11	0.40	0.47
2014_IALG	142	MC	05	1	597	0.62	0.05		0.06	0.08	0.79	0.03	0.79	0.37
2014_IALG	142	MC	06	1	597	0.62	0.06		0.69	0.09	0.12	0.04	0.69	0.27

Test	Form	Type	Item	Max	N-Count	Alpha	B	M0	M1	M2	M3	M4	Mean	Point-Biserial
2014_IALG	142	MC	07	1	597	0.62	0.07		0.14	0.49	0.13	0.18	0.49	0.53
2014_IALG	142	MC	08	1	597	0.62	0.07		0.31	0.35	0.11	0.15	0.31	0.36
2014_IALG	142	CR	09	4	597	0.62	0.09	0.76	0.04	0.02	0.05	0.04	0.39	0.61
2014_IALG	142	CR	10	2	597	0.62	0.14	0.49	0.05	0.32			0.69	0.62
2014_IALG	142	CR	11	3	597	0.62	0.20	0.69	0.05	0.04	0.02		0.18	0.45
2014_IALG	143	MC	01	1	601	0.68	0.06		0.07	0.74	0.10	0.02	0.74	0.47
2014_IALG	143	MC	02	1	601	0.68	0.06		0.50	0.06	0.32	0.05	0.32	0.49
2014_IALG	143	MC	03	1	601	0.68	0.08		0.13	0.16	0.16	0.47	0.47	0.52
2014_IALG	143	MC	04	1	601	0.68	0.06		0.26	0.23	0.40	0.05	0.40	0.46
2014_IALG	143	MC	05	1	601	0.68	0.08		0.39	0.27	0.16	0.10	0.39	0.32
2014_IALG	143	MC	06	1	601	0.68	0.08		0.13	0.46	0.23	0.11	0.46	0.43
2014_IALG	143	MC	07	1	601	0.68	0.06		0.44	0.07	0.37	0.06	0.44	0.35
2014_IALG	143	MC	08	1	601	0.68	0.08		0.20	0.09	0.09	0.54	0.54	0.53
2014_IALG	143	CR	09	2	601	0.68	0.13	0.39	0.14	0.34			0.82	0.64
2014_IALG	143	CR	10	3	601	0.68	0.17	0.52	0.18	0.03	0.09		0.52	0.63
2014_IALG	143	CR	11	4	601	0.68	0.27	0.62	0.03	0.04	0.02	0.02	0.25	0.52
2014_IALG	144	MC	01	1	594	0.68	0.05		0.08	0.08	0.43	0.36	0.43	0.56
2014_IALG	144	MC	02	1	594	0.68	0.07		0.15	0.28	0.28	0.23	0.23	0.42
2014_IALG	144	MC	03	1	594	0.68	0.07		0.16	0.29	0.38	0.09	0.38	0.47
2014_IALG	144	MC	04	1	594	0.68	0.05		0.06	0.37	0.48	0.04	0.37	0.42
2014_IALG	144	MC	05	1	594	0.68	0.06		0.31	0.28	0.16	0.20	0.28	0.41
2014_IALG	144	MC	06	1	594	0.68	0.05		0.03	0.17	0.69	0.06	0.69	0.52
2014_IALG	144	MC	07	1	594	0.68	0.06		0.66	0.14	0.12	0.02	0.66	0.47
2014_IALG	144	MC	08	1	594	0.68	0.07		0.12	0.17	0.09	0.54	0.54	0.47
2014_IALG	144	CR	09	4	594	0.68	0.11	0.70	0.04	0.04	0.03	0.08	0.54	0.62
2014_IALG	144	CR	10	2	594	0.68	0.13	0.25	0.21	0.41			1.02	0.63
2014_IALG	144	CR	11	3	594	0.68	0.19	0.67	0.08	0.02	0.04		0.24	0.53
2014_IALG	145	MC	01	1	594	0.62	0.06		0.19	0.19	0.41	0.15	0.41	0.41

Test	Form	Type	Item	Max	N-Count	Alpha	B	M0	M1	M2	M3	M4	Mean	Point-Biserial
2014_IALG	145	MC	02	1	594	0.62	0.06		0.35	0.32	0.16	0.11	0.32	0.33
2014_IALG	145	MC	03	1	594	0.62	0.05		0.29	0.35	0.21	0.10	0.35	0.31
2014_IALG	145	MC	04	1	594	0.62	0.04		0.08	0.12	0.16	0.59	0.59	0.46
2014_IALG	145	MC	05	1	594	0.62	0.05		0.10	0.13	0.27	0.45	0.27	0.18
2014_IALG	145	MC	06	1	594	0.62	0.04		0.03	0.03	0.09	0.81	0.81	0.41
2014_IALG	145	MC	07	1	594	0.62	0.08		0.37	0.27	0.19	0.09	0.37	0.39
2014_IALG	145	MC	08	1	594	0.62	0.08		0.10	0.66	0.11	0.05	0.66	0.48
2014_IALG	145	CR	09	2	594	0.62	0.12	0.21	0.44	0.23			0.90	0.53
2014_IALG	145	CR	10	3	594	0.62	0.11	0.48	0.32	0.05	0.04		0.54	0.65
2014_IALG	145	CR	11	4	594	0.62	0.19	0.52	0.14	0.07	0.04	0.04	0.55	0.70
2014_IALG	146	MC	01	1	612	0.68	0.07		0.23	0.15	0.47	0.08	0.47	0.47
2014_IALG	146	MC	02	1	612	0.68	0.06		0.26	0.06	0.48	0.14	0.48	0.41
2014_IALG	146	MC	03	1	612	0.68	0.06		0.35	0.04	0.03	0.53	0.53	0.49
2014_IALG	146	MC	04	1	612	0.68	0.07		0.38	0.25	0.17	0.14	0.38	0.32
2014_IALG	146	MC	05	1	612	0.68	0.07		0.13	0.15	0.35	0.30	0.30	0.48
2014_IALG	146	MC	06	1	612	0.68	0.06		0.19	0.12	0.15	0.47	0.47	0.47
2014_IALG	146	MC	07	1	612	0.68	0.07		0.06	0.30	0.15	0.42	0.30	0.33
2014_IALG	146	MC	08	1	612	0.68	0.07		0.07	0.64	0.05	0.16	0.64	0.49
2014_IALG	146	CR	09	2	612	0.68	0.08	0.39	0.21	0.31			0.84	0.56
2014_IALG	146	CR	10	3	612	0.68	0.12	0.49	0.17	0.05	0.17		0.79	0.61
2014_IALG	146	CR	11	4	612	0.68	0.16	0.30	0.01	0.27	0.03	0.23	1.56	0.78
2014_IALG	147	MC	01	1	612	0.63	0.06		0.51	0.17	0.16	0.11	0.51	0.36
2014_IALG	147	MC	02	1	612	0.63	0.04		0.12	0.08	0.06	0.70	0.70	0.43
2014_IALG	147	MC	03	1	612	0.63	0.05		0.26	0.48	0.13	0.08	0.48	0.44
2014_IALG	147	MC	04	1	612	0.63	0.05		0.08	0.25	0.54	0.08	0.54	0.41
2014_IALG	147	MC	05	1	612	0.63	0.04		0.03	0.22	0.59	0.12	0.59	0.51
2014_IALG	147	MC	06	1	612	0.63	0.05		0.07	0.24	0.56	0.08	0.24	0.34
2014_IALG	147	MC	07	1	612	0.63	0.07		0.15	0.22	0.34	0.22	0.34	0.39

Test	Form	Type	Item	Max	N-Count	Alpha	B	M0	M1	M2	M3	M4	Mean	Point-Biserial
2014_IALG	147	MC	08	1	612	0.63	0.07		0.12	0.17	0.18	0.46	0.46	0.50
2014_IALG	147	CR	09	4	612	0.63	0.13	0.48	0.07	0.18	0.05	0.09	0.95	0.71
2014_IALG	147	CR	10	2	612	0.63	0.19	0.56	0.17	0.08			0.33	0.49
2014_IALG	147	CR	11	2	612	0.63	0.16	0.06	0.22	0.56			1.35	0.53
2014_IALG	148	MC	01	1	618	0.63	0.08		0.22	0.27	0.38	0.06	0.38	0.34
2014_IALG	148	MC	02	1	618	0.63	0.06		0.10	0.13	0.24	0.46	0.46	0.40
2014_IALG	148	MC	03	1	618	0.63	0.08		0.43	0.24	0.14	0.12	0.43	0.44
2014_IALG	148	MC	04	1	618	0.63	0.06		0.03	0.41	0.38	0.10	0.38	0.27
2014_IALG	148	MC	05	1	618	0.63	0.07		0.10	0.58	0.21	0.05	0.21	0.28
2014_IALG	148	MC	06	1	618	0.63	0.08		0.22	0.14	0.25	0.31	0.31	0.33
2014_IALG	148	MC	07	1	618	0.63	0.09		0.17	0.12	0.36	0.25	0.36	0.46
2014_IALG	148	MC	08	1	618	0.63	0.09		0.11	0.58	0.17	0.05	0.58	0.50
2014_IALG	148	CR	09	4	618	0.63	0.08	0.20	0.21	0.19	0.06	0.27	1.83	0.76
2014_IALG	148	CR	10	2	618	0.63	0.18	0.42	0.12	0.28			0.67	0.55
2014_IALG	148	CR	11	3	618	0.63	0.20	0.56	0.08	0.04	0.12		0.52	0.66
2014_IALG	149	MC	01	1	601	0.69	0.06		0.15	0.24	0.26	0.28	0.28	0.31
2014_IALG	149	MC	02	1	601	0.69	0.06		0.19	0.44	0.19	0.11	0.44	0.41
2014_IALG	149	MC	03	1	601	0.69	0.08		0.17	0.31	0.20	0.23	0.31	0.31
2014_IALG	149	MC	04	1	601	0.69	0.08		0.17	0.20	0.20	0.35	0.35	0.54
2014_IALG	149	MC	05	1	601	0.69	0.06		0.12	0.69	0.07	0.06	0.69	0.38
2014_IALG	149	MC	06	1	601	0.69	0.07		0.38	0.08	0.07	0.40	0.40	0.58
2014_IALG	149	MC	07	1	601	0.69	0.06		0.35	0.46	0.09	0.04	0.35	0.51
2014_IALG	149	MC	08	1	601	0.69	0.08		0.41	0.16	0.18	0.17	0.41	0.46
2014_IALG	149	CR	09	2	601	0.69	0.12	0.47	0.19	0.22			0.63	0.67
2014_IALG	149	CR	10	3	601	0.69	0.21	0.69	0.06	0.01	0.03		0.16	0.53
2014_IALG	149	CR	11	3	601	0.69	0.22	0.50	0.13	0.07	0.08		0.51	0.68
2014_IALG	150	MC	01	1	605	0.62	0.07		0.12	0.70	0.06	0.05	0.70	0.35
2014_IALG	150	MC	02	1	605	0.62	0.07		0.17	0.21	0.17	0.38	0.38	0.46

Test	Form	Type	Item	Max	N-Count	Alpha	B	M0	M1	M2	M3	M4	Mean	Point-Biserial
2014_IALG	150	MC	03	1	605	0.62	0.07		0.49	0.16	0.19	0.09	0.49	0.46
2014_IALG	150	MC	04	1	605	0.62	0.07		0.55	0.08	0.26	0.04	0.26	0.32
2014_IALG	150	MC	05	1	605	0.62	0.09		0.12	0.36	0.21	0.21	0.36	0.40
2014_IALG	150	MC	06	1	605	0.62	0.09		0.38	0.32	0.14	0.07	0.38	0.46
2014_IALG	150	MC	07	1	605	0.62	0.07		0.09	0.06	0.61	0.16	0.61	0.44
2014_IALG	150	MC	08	1	605	0.62	0.09		0.16	0.49	0.08	0.18	0.49	0.48
2014_IALG	150	CR	09	3	605	0.62	0.13	0.75	0.06	0.05	0.01		0.19	0.52
2014_IALG	150	CR	10	4	605	0.62	0.16	0.66	0.03	0.04	0.05	0.06	0.49	0.61
2014_IALG	150	CR	11	2	605	0.62	0.22	0.51	0.13	0.13			0.40	0.58
2014_IALG	151	MC	01	1	593	0.72	0.07		0.19	0.21	0.14	0.38	0.38	0.47
2014_IALG	151	MC	02	1	593	0.72	0.05		0.05	0.50	0.29	0.11	0.50	0.52
2014_IALG	151	MC	03	1	593	0.72	0.07		0.11	0.20	0.49	0.13	0.49	0.46
2014_IALG	151	MC	04	1	593	0.72	0.09		0.24	0.27	0.26	0.13	0.24	0.22
2014_IALG	151	MC	05	1	593	0.72	0.06		0.05	0.33	0.12	0.44	0.44	0.45
2014_IALG	151	MC	06	1	593	0.72	0.05		0.13	0.49	0.26	0.06	0.49	0.56
2014_IALG	151	MC	07	1	593	0.72	0.07		0.18	0.11	0.61	0.04	0.61	0.46
2014_IALG	151	MC	08	1	593	0.72	0.09		0.10	0.11	0.38	0.32	0.32	0.54
2014_IALG	151	CR	09	2	593	0.72	0.15	0.39	0.24	0.22			0.68	0.64
2014_IALG	151	CR	10	3	593	0.72	0.20	0.56	0.10	0.07	0.07		0.45	0.64
2014_IALG	151	CR	11	4	593	0.72	0.17	0.37	0.18	0.17	0.06	0.04	0.90	0.68
2014_IALG	152	MC	01	1	596	0.69	0.05		0.18	0.04	0.28	0.45	0.45	0.54
2014_IALG	152	MC	02	1	596	0.69	0.06		0.10	0.44	0.35	0.06	0.44	0.52
2014_IALG	152	MC	03	1	596	0.69	0.08		0.12	0.33	0.31	0.17	0.17	0.37
2014_IALG	152	MC	04	1	596	0.69	0.06		0.39	0.09	0.24	0.21	0.24	0.43
2014_IALG	152	MC	05	1	596	0.69	0.06		0.10	0.15	0.39	0.30	0.39	0.49
2014_IALG	152	MC	06	1	596	0.69	0.06		0.55	0.11	0.12	0.16	0.55	0.47
2014_IALG	152	MC	07	1	596	0.69	0.07		0.11	0.58	0.21	0.03	0.58	0.45
2014_IALG	152	MC	08	1	596	0.69	0.08		0.16	0.07	0.60	0.10	0.60	0.43

Test	Form	Type	Item	Max	N-Count	Alpha	B	M0	M1	M2	M3	M4	Mean	Point-Biserial
2014_IALG	152	CR	09	2	596	0.69	0.09	0.28	0.10	0.53			1.15	0.62
2014_IALG	152	CR	10	3	596	0.69	0.12	0.22	0.15	0.22	0.29		1.47	0.65
2014_IALG	152	CR	11	4	596	0.69	0.13	0.73	0.02	0.04	0.02	0.06	0.39	0.61
2014_IALG	153	MC	01	1	584	0.65	0.05		0.57	0.05	0.27	0.06	0.57	0.47
2014_IALG	153	MC	02	1	584	0.65	0.07		0.09	0.38	0.39	0.08	0.39	0.35
2014_IALG	153	MC	03	1	584	0.65	0.07		0.07	0.17	0.53	0.16	0.53	0.38
2014_IALG	153	MC	04	1	584	0.65	0.06		0.14	0.47	0.08	0.24	0.47	0.36
2014_IALG	153	MC	05	1	584	0.65	0.06		0.10	0.13	0.14	0.57	0.57	0.45
2014_IALG	153	MC	06	1	584	0.65	0.06		0.45	0.13	0.13	0.23	0.23	0.56
2014_IALG	153	MC	07	1	584	0.65	0.09		0.27	0.17	0.27	0.20	0.27	0.39
2014_IALG	153	MC	08	1	584	0.65	0.08		0.17	0.40	0.15	0.21	0.40	0.32
2014_IALG	153	CR	09	3	584	0.65	0.17	0.36	0.14	0.08	0.25		1.05	0.73
2014_IALG	153	CR	10	4	584	0.65	0.18	0.27	0.02	0.18	0.13	0.21	1.63	0.77
2014_IALG	153	CR	11	2	584	0.65	0.27	0.55	0.09	0.09			0.26	0.44
2014_IALG	154	MC	01	1	579	0.53	0.04		0.15	0.46	0.27	0.07	0.46	0.41
2014_IALG	154	MC	02	1	579	0.53	0.05		0.19	0.20	0.42	0.13	0.42	0.45
2014_IALG	154	MC	03	1	579	0.53	0.05		0.31	0.18	0.11	0.35	0.35	0.45
2014_IALG	154	MC	04	1	579	0.53	0.06		0.18	0.44	0.22	0.11	0.44	0.40
2014_IALG	154	MC	05	1	579	0.53	0.06		0.26	0.22	0.25	0.21	0.26	0.00
2014_IALG	154	MC	06	1	579	0.53	0.05		0.22	0.29	0.33	0.11	0.33	0.37
2014_IALG	154	MC	07	1	579	0.53	0.06		0.05	0.65	0.19	0.06	0.65	0.45
2014_IALG	154	MC	08	1	579	0.53	0.07		0.25	0.29	0.21	0.18	0.29	0.46
2014_IALG	154	CR	09	4	579	0.53	0.13	0.50	0.14	0.06	0.04	0.14	0.92	0.75
2014_IALG	154	CR	10	.										
2014_IALG	154	CR	11	3	579	0.53	0.23	0.63	0.07	0.05	0.02		0.22	0.53
2014_IALG	155	MC	01	1	589	0.68	0.04		0.12	0.07	0.04	0.72	0.72	0.46
2014_IALG	155	MC	02	1	589	0.68	0.06		0.35	0.27	0.15	0.16	0.35	0.37
2014_IALG	155	MC	03	1	589	0.68	0.05		0.09	0.29	0.20	0.38	0.38	0.48

Test	Form	Type	Item	Max	N-Count	Alpha	B	M0	M1	M2	M3	M4	Mean	Point-Biserial
2014_IALG	155	MC	04	1	589	0.68	0.06		0.19	0.41	0.23	0.13	0.41	0.49
2014_IALG	155	MC	05	1	589	0.68	0.06		0.18	0.27	0.33	0.15	0.33	0.48
2014_IALG	155	MC	06	1	589	0.68	0.06		0.11	0.57	0.13	0.13	0.57	0.45
2014_IALG	155	MC	07	1	589	0.68	0.07		0.19	0.32	0.20	0.22	0.20	0.27
2014_IALG	155	MC	08	1	589	0.68	0.08		0.06	0.19	0.56	0.10	0.56	0.43
2014_IALG	155	CR	09	3	589	0.68	0.29	0.59	0.04	0.04	0.04		0.23	0.63
2014_IALG	155	CR	10	4	589	0.68	0.23	0.63	0.04	0.01	0.00	0.08	0.40	0.70
2014_IALG	155	CR	11	2	589	0.68	0.21	0.40	0.26	0.14			0.54	0.54
2014_IALG	156	MC	01	1	576	0.68	0.05		0.40	0.05	0.33	0.18	0.33	0.51
2014_IALG	156	MC	02	1	576	0.68	0.05		0.43	0.20	0.17	0.15	0.43	0.42
2014_IALG	156	MC	03	1	576	0.68	0.06		0.50	0.17	0.16	0.11	0.50	0.54
2014_IALG	156	MC	04	1	576	0.68	0.05		0.14	0.72	0.05	0.04	0.72	0.48
2014_IALG	156	MC	05	1	576	0.68	0.07		0.17	0.14	0.18	0.44	0.44	0.21
2014_IALG	156	MC	06	1	576	0.68	0.05		0.05	0.26	0.36	0.28	0.28	0.48
2014_IALG	156	MC	07	1	576	0.68	0.06		0.10	0.10	0.61	0.12	0.61	0.43
2014_IALG	156	MC	08	1	576	0.68	0.06		0.59	0.06	0.26	0.04	0.26	0.49
2014_IALG	156	CR	09	4	576	0.68	0.10	0.45	0.06	0.08	0.07	0.23	1.36	0.81
2014_IALG	156	CR	10	3	576	0.68	0.24	0.61	0.06	0.01	0.08		0.32	0.61
2014_IALG	156	CR	11	2	576	0.68	0.17	0.31	0.30	0.22			0.75	0.52
2014_IALG	157	MC	01	1	575	0.67	0.05		0.18	0.18	0.41	0.19	0.41	0.39
2014_IALG	157	MC	02	1	575	0.67	0.05		0.10	0.43	0.27	0.14	0.43	0.38
2014_IALG	157	MC	03	1	575	0.67	0.05		0.10	0.11	0.52	0.21	0.21	0.40
2014_IALG	157	MC	04	1	575	0.67	0.05		0.10	0.12	0.42	0.32	0.42	0.51
2014_IALG	157	MC	05	1	575	0.67	0.06		0.13	0.09	0.27	0.46	0.09	0.29
2014_IALG	157	MC	06	1	575	0.67	0.06		0.11	0.53	0.25	0.05	0.53	0.31
2014_IALG	157	MC	07	1	575	0.67	0.06		0.15	0.22	0.16	0.42	0.42	0.57
2014_IALG	157	MC	08	1	575	0.67	0.07		0.44	0.29	0.14	0.05	0.44	0.40
2014_IALG	157	CR	09	2	575	0.67	0.09	0.22	0.10	0.59			1.29	0.60

Test	Form	Type	Item	Max	N-Count	Alpha	B	M0	M1	M2	M3	M4	Mean	Point-Biserial
2014_IALG	157	CR	10	3	575	0.67	0.13	0.23	0.08	0.18	0.38		1.58	0.69
2014_IALG	157	CR	11	4	575	0.67	0.16	0.56	0.08	0.04	0.02	0.14	0.77	0.73

Appendix B: Inter-Rater Consistency – Point Differences Between First and Second Reads

The first three columns form the left contain the form ID, item sequence number, and number of score points for each item. The remaining columns contain the percentage of times each possible difference between the first and second raters' scores occurred. Blank cells indicate out-of-range differences (e.g., differences greater than the maximum possible given the point value of that particular item).

Form	Item	Score Points	Difference (First Read Minus Second Read)								
			−4	−3	−2	−1	0	1	2	3	4
141	09	2			0%	3%	95%	2%	0%		
141	10	3		0%	3%	1%	93%	1%	3%	0%	
141	11	4	0%	0%	1%	5%	86%	5%	2%	0%	0%
142	09	4	0%	0%	0%	4%	92%	4%	0%	0%	0%
142	10	2			0%	1%	96%	3%	0%		
142	11	3		0%	2%	5%	92%	1%	1%	0%	
143	09	2			0%	5%	87%	6%	2%		
143	10	3		0%	1%	7%	83%	8%	1%	0%	
143	11	4	0%	0%	1%	4%	90%	2%	3%	0%	0%
144	09	4	0%	0%	5%	1%	86%	5%	4%	0%	0%
144	10	2			0%	8%	88%	4%	0%		
144	11	3		0%	0%	4%	89%	7%	0%	0%	
145	09	2			0%	6%	86%	8%	0%		
145	10	3		0%	0%	8%	85%	7%	0%	0%	
145	11	4	0%	0%	2%	4%	85%	6%	3%	0%	0%
146	09	2			0%	4%	93%	3%	1%		
146	10	3		0%	0%	6%	88%	4%	2%	0%	
146	11	4	0%	0%	5%	2%	89%	1%	4%	0%	0%
147	09	4	0%	0%	2%	7%	74%	12%	6%	0%	0%
147	10	2			0%	3%	93%	4%	0%		
147	11	2			0%	5%	90%	6%	0%		
148	09	4	0%	0%	2%	11%	76%	10%	0%	0%	0%
148	10	2			0%	10%	82%	8%	0%		
148	11	3		0%	1%	5%	90%	3%	2%	0%	
149	09	2			0%	12%	78%	10%	0%		
149	10	3		0%	3%	2%	93%	1%	1%	0%	
149	11	3		0%	0%	3%	92%	4%	1%	0%	
150	09	3		0%	1%	3%	90%	6%	1%	0%	
150	10	4	0%	0%	1%	3%	88%	7%	1%	0%	0%
150	11	2			1%	8%	87%	4%	1%		

Form	Item	Score Points	Difference (First Read Minus Second Read)								
			−4	−3	−2	−1	0	1	2	3	4
151	09	2			0%	3%	94%	3%	0%		
151	10	3		0%	1%	8%	83%	7%	1%	0%	
151	11	4	0%	0%	0%	2%	95%	3%	0%	0%	0%
152	09	2			1%	6%	91%	1%	1%		
152	10	3		0%	3%	16%	62%	18%	1%	0%	
152	11	4	0%	0%	0%	2%	92%	4%	3%	0%	0%
153	09	3		0%	0%	5%	90%	5%	0%	0%	
153	10	4	0%	0%	8%	1%	87%	3%	1%	0%	0%
153	11	2			0%	3%	97%	0%	0%		
154	09	4	0%	0%	3%	6%	81%	11%	0%	0%	0%
154	11	3		0%	2%	5%	85%	5%	3%	0%	
155	09	3		0%	0%	2%	94%	3%	1%	0%	
155	10	4	0%	0%	2%	2%	94%	1%	1%	0%	0%
155	11	2			0%	2%	94%	4%	0%		
156	09	4	0%	0%	0%	6%	85%	6%	4%	0%	0%
156	10	3		0%	0%	1%	92%	5%	2%	0%	
156	11	2			0%	6%	88%	7%	0%		
157	09	2			0%	4%	91%	5%	0%		
157	10	3		0%	3%	5%	78%	11%	4%	0%	
157	11	4	0%	0%	0%	1%	93%	7%	0%	0%	0%

Appendix C: Additional Measures of Inter-rater Reliability and Agreement

The first four columns from the left contain the form ID, item sequence number, number of score points, and the total count of items receiving a first and second read. In the fifth column, the percent of exact matches between the first and second scores is provided. The following column ("Adj.") is the percentage of the first and second scores with a difference of −1 or 1. "Total" is the sum of Exact and Adjacent matches (e.g., the two prior columns).

Form	Item	Score Points	Total N-Count	Agreement (%)			Raw Score Mean		Raw Score Standard Deviation		Intraclass Corr.	Weighted Kappa
				Exact	Adj.	Total	First Read	Second Read	First Read	Second Read		
141	09	2	107	95.3%	4.7%	100.0%	1.1	1.1	0.94	0.92	0.97	0.95
141	10	3	108	92.6%	1.9%	94.4%	1.4	1.4	1.09	1.10	0.90	0.89
141	11	4	110	86.4%	10.9%	97.3%	0.7	0.8	1.24	1.29	0.93	0.86
142	09	4	101	92.1%	7.9%	100.0%	0.4	0.4	1.02	1.00	0.96	0.88
142	10	2	107	96.3%	3.7%	100.0%	0.8	0.8	0.97	0.96	0.98	0.96
142	11	3	106	91.5%	5.7%	97.2%	0.2	0.2	0.63	0.67	0.80	0.70
143	09	2	108	87.0%	11.1%	98.1%	0.9	0.8	0.95	0.93	0.90	0.85
143	10	3	107	83.2%	15.0%	98.1%	0.6	0.6	0.94	0.95	0.87	0.78
143	11	4	104	90.4%	5.8%	96.2%	0.3	0.2	0.78	0.78	0.83	0.71
144	09	4	105	85.7%	5.7%	91.4%	0.6	0.6	1.26	1.27	0.87	0.78
144	10	2	110	88.2%	11.8%	100.0%	1.1	1.2	0.91	0.90	0.93	0.88
144	11	3	104	89.4%	10.6%	100.0%	0.3	0.2	0.70	0.67	0.89	0.76
145	09	2	106	85.8%	14.2%	100.0%	1.0	1.0	0.77	0.78	0.88	0.83
145	10	3	107	85.0%	15.0%	100.0%	0.6	0.6	0.85	0.87	0.90	0.82
145	11	4	109	85.3%	10.1%	95.4%	0.8	0.7	1.20	1.19	0.90	0.83
146	09	2	111	92.8%	6.3%	99.1%	0.8	0.8	0.84	0.83	0.93	0.91
146	10	3	109	88.1%	10.1%	98.2%	0.7	0.6	1.03	1.00	0.92	0.85
146	11	4	110	89.1%	2.7%	91.8%	1.6	1.6	1.60	1.60	0.93	0.89
147	09	4	106	73.6%	18.9%	92.5%	1.0	0.9	1.34	1.26	0.86	0.74
147	10	2	105	93.3%	6.7%	100.0%	0.5	0.5	0.75	0.75	0.94	0.90

Form	Item	Score Points	Total N-Count	Agreement (%)			Raw Score Mean		Raw Score Standard Deviation		Intraclass Corr.	Weighted Kappa
				Exact	Adj.	Total	First Read	Second Read	First Read	Second Read		
147	11	2	106	89.6%	10.4%	100.0%	1.5	1.5	0.72	0.72	0.90	0.84
148	09	4	106	76.4%	21.7%	98.1%	1.9	1.9	1.61	1.58	0.94	0.86
148	10	2	112	82.1%	17.9%	100.0%	0.5	0.5	0.81	0.80	0.86	0.76
148	11	3	111	90.1%	7.2%	97.3%	0.6	0.6	1.15	1.12	0.93	0.87
149	09	2	109	78.0%	22.0%	100.0%	0.6	0.7	0.82	0.83	0.84	0.74
149	10	3	102	93.1%	2.9%	96.1%	0.2	0.3	0.70	0.78	0.83	0.75
149	11	3	105	92.4%	6.7%	99.0%	0.6	0.6	0.99	0.97	0.95	0.90
150	09	3	107	89.7%	8.4%	98.1%	0.3	0.3	0.70	0.70	0.84	0.75
150	10	4	103	88.3%	9.7%	98.1%	0.6	0.5	1.23	1.15	0.94	0.85
150	11	2	106	86.8%	11.3%	98.1%	0.4	0.4	0.65	0.73	0.80	0.75
151	09	2	104	94.2%	5.8%	100.0%	0.6	0.6	0.82	0.83	0.96	0.93
151	10	3	109	82.6%	15.6%	98.2%	0.6	0.6	0.99	1.02	0.89	0.78
151	11	4	106	95.3%	4.7%	100.0%	0.9	0.9	1.23	1.22	0.98	0.96
152	09	2	109	90.8%	7.3%	98.2%	1.0	1.1	0.94	0.92	0.92	0.89
152	10	3	106	62.3%	34.0%	96.2%	1.5	1.6	1.16	1.11	0.81	0.67
152	11	4	108	91.7%	5.6%	97.2%	0.4	0.3	0.98	0.89	0.90	0.81
153	09	3	105	90.5%	9.5%	100.0%	1.3	1.3	1.33	1.36	0.97	0.93
153	10	4	106	86.8%	3.8%	90.6%	1.8	1.9	1.75	1.69	0.93	0.88
153	11	2	102	97.1%	2.9%	100.0%	0.3	0.3	0.66	0.67	0.97	0.94
154	09	4	103	80.6%	16.5%	97.1%	1.0	1.0	1.47	1.43	0.93	0.84
154	11	3	101	85.1%	9.9%	95.0%	0.2	0.2	0.55	0.54	0.50	0.44
155	09	3	104	94.2%	4.8%	99.0%	0.3	0.2	0.72	0.73	0.92	0.85
155	10	4	106	94.3%	2.8%	97.2%	0.4	0.5	1.15	1.15	0.95	0.89
155	11	2	102	94.1%	5.9%	100.0%	0.5	0.5	0.71	0.74	0.94	0.92
156	09	4	104	84.6%	11.5%	96.2%	1.7	1.7	1.80	1.82	0.96	0.90
156	10	3	103	92.2%	5.8%	98.1%	0.4	0.3	0.95	0.90	0.92	0.85

Form	Item	Score Points	Total N-Count	Agreement (%)			Raw Score Mean		Raw Score Standard Deviation		Intraclass Corr.	Weighted Kappa
				Exact	Adj.	Total	First Read	Second Read	First Read	Second Read		
156	11	2	104	87.5%	12.5%	100.0%	0.7	0.7	0.77	0.79	0.90	0.85
157	09	2	104	91.3%	8.7%	100.0%	1.2	1.2	0.90	0.91	0.95	0.91
157	10	3	104	77.9%	15.4%	93.3%	1.8	1.7	1.30	1.26	0.87	0.79
157	11	4	107	92.5%	7.5%	100.0%	1.0	0.9	1.58	1.59	0.99	0.95

Appendix D: Partial-Credit Model Item Analysis

The first five columns from the left contain the test name, form name, item type, item number on the form, and maximum points possible for the item. The sixth column contains the number of students that the item was administered to. The remaining six columns contain the Rasch Item Difficulty, step difficulties (for multi-point items only), and the INFIT Rasch model fit statistic. Items without statistics are DNS (Do Not Score) status items.

Test	Form	Type	Item	Max	N-Count	RID	S1	S2	S3	S4	INFIT
2014_IALG	141	MC	01	1	598	−1.1968					0.99
2014_IALG	141	MC	02	1	598	1.4119					0.96
2014_IALG	141	MC	03	1	598	−0.9080					0.98
2014_IALG	141	MC	04	1	598	0.6391					0.94
2014_IALG	141	MC	05	1	598	0.3472					1.17
2014_IALG	141	MC	06	1	598	−0.5505					0.85
2014_IALG	141	MC	07	1	598	−0.5006					0.99
2014_IALG	141	MC	08	1	598	−1.5523					0.90
2014_IALG	141	CR	09	2	598	−0.5216	0.4328	−0.4328			1.04
2014_IALG	141	CR	10	3	598	0.0969	1.8832	−3.4884	1.6052		1.12
2014_IALG	141	CR	11	4	598	1.0358	0.3433	0.2411	0.5421	−1.1265	0.99
2014_IALG	142	MC	01	1	597	0.3738					0.89
2014_IALG	142	MC	02	1	597	0.9131					1.07
2014_IALG	142	MC	03	1	597	−0.3429					0.99
2014_IALG	142	MC	04	1	597	0.1037					0.95
2014_IALG	142	MC	05	1	597	−1.9711					1.01
2014_IALG	142	MC	06	1	597	−1.3543					1.08
2014_IALG	142	MC	07	1	597	−0.3187					0.90
2014_IALG	142	MC	08	1	597	0.5414					1.07
2014_IALG	142	CR	09	4	597	1.2667	1.6110	−0.3636	−1.2721	0.0247	0.95
2014_IALG	142	CR	10	2	597	0.1853	1.8423	−1.8423			0.96
2014_IALG	142	CR	11	3	597	1.7605	1.0366	−0.8874	−0.1492		1.05
2014_IALG	143	MC	01	1	601	−1.7185					0.95
2014_IALG	143	MC	02	1	601	0.4960					0.95
2014_IALG	143	MC	03	1	601	−0.2590					0.93
2014_IALG	143	MC	04	1	601	0.0713					1.01
2014_IALG	143	MC	05	1	601	0.1470					1.17
2014_IALG	143	MC	06	1	601	−0.1935					1.05
2014_IALG	143	MC	07	1	601	−0.1113					1.12
2014_IALG	143	MC	08	1	601	−0.6119					0.90
2014_IALG	143	CR	09	2	601	−0.0331	0.6754	−0.6754			0.96

Test	Form	Type	Item	Max	N-Count	RID	S1	S2	S3	S4	INFIT
2014_IALG	143	CR	10	3	601	0.9711	−0.0471	1.0457	−0.9986		0.99
2014_IALG	143	CR	11	4	601	1.6857	1.6422	−1.6512	0.2314	−0.2223	0.94
2014_IALG	144	MC	01	1	594	−0.0404					0.89
2014_IALG	144	MC	02	1	594	1.0971					1.01
2014_IALG	144	MC	03	1	594	0.1944					0.99
2014_IALG	144	MC	04	1	594	0.2741					1.06
2014_IALG	144	MC	05	1	594	0.7806					1.05
2014_IALG	144	MC	06	1	594	−1.4570					0.88
2014_IALG	144	MC	07	1	594	−1.2360					0.98
2014_IALG	144	MC	08	1	594	−0.6159					1.02
2014_IALG	144	CR	09	4	594	1.0920	1.5172	−0.6972	0.1998	−1.0198	1.12
2014_IALG	144	CR	10	2	594	−0.4294	0.1682	−0.1682			0.98
2014_IALG	144	CR	11	3	594	1.5762	0.6929	0.6116	−1.3046		0.98
2014_IALG	145	MC	01	1	594	0.0938					1.02
2014_IALG	145	MC	02	1	594	0.5408					1.09
2014_IALG	145	MC	03	1	594	0.4273					1.11
2014_IALG	145	MC	04	1	594	−0.7648					0.94
2014_IALG	145	MC	05	1	594	0.8570					1.21
2014_IALG	145	MC	06	1	594	−2.0021					0.92
2014_IALG	145	MC	07	1	594	0.2915					1.04
2014_IALG	145	MC	08	1	594	−1.1237					0.90
2014_IALG	145	CR	09	2	594	−0.0648	−0.8525	0.8525			1.02
2014_IALG	145	CR	10	3	594	1.1876	−0.9628	1.0167	−0.0539		0.87
2014_IALG	145	CR	11	4	594	1.2056	0.0557	−0.2786	0.0876	0.1353	0.77
2014_IALG	146	MC	01	1	612	−0.2450					0.98
2014_IALG	146	MC	02	1	612	−0.2918					1.05
2014_IALG	146	MC	03	1	612	−0.5184					0.94
2014_IALG	146	MC	04	1	612	0.2071					1.11
2014_IALG	146	MC	05	1	612	0.5985					0.93
2014_IALG	146	MC	06	1	612	−0.2528					0.96
2014_IALG	146	MC	07	1	612	0.6075					1.08
2014_IALG	146	MC	08	1	612	−1.1067					0.93
2014_IALG	146	CR	09	2	612	−0.0629	0.2473	−0.2473			1.06
2014_IALG	146	CR	10	3	612	0.4348	0.3050	0.9283	−1.2333		1.11
2014_IALG	146	CR	11	4	612	0.0094	3.4014	−4.0469	2.3775	−1.7319	0.88
2014_IALG	147	MC	01	1	612	−0.3643					1.07
2014_IALG	147	MC	02	1	612	−1.2979					0.96
2014_IALG	147	MC	03	1	612	−0.2618					0.99
2014_IALG	147	MC	04	1	612	−0.5112					1.00
2014_IALG	147	MC	05	1	612	−0.7347					0.90

Test	Form	Type	Item	Max	N-Count	RID	S1	S2	S3	S4	INFIT
2014_IALG	147	MC	06	1	612	0.9563					1.05
2014_IALG	147	MC	07	1	612	0.4063					1.04
2014_IALG	147	MC	08	1	612	−0.1443					0.92
2014_IALG	147	CR	09	4	612	0.5992	0.9819	−1.6403	1.0050	−0.3466	0.97
2014_IALG	147	CR	10	2	612	1.2032	−0.0661	0.0661			1.09
2014_IALG	147	CR	11	2	612	−1.0007	0.1002	−0.1002			1.02
2014_IALG	148	MC	01	1	618	0.2079					1.07
2014_IALG	148	MC	02	1	618	−0.2067					1.01
2014_IALG	148	MC	03	1	618	−0.0325					0.98
2014_IALG	148	MC	04	1	618	0.1921					1.14
2014_IALG	148	MC	05	1	618	1.1693					1.08
2014_IALG	148	MC	06	1	618	0.5704					1.07
2014_IALG	148	MC	07	1	618	0.2795					0.95
2014_IALG	148	MC	08	1	618	−0.7366					0.91
2014_IALG	148	CR	09	4	618	−0.2858	−0.4190	−0.0454	1.4336	−0.9693	0.85
2014_IALG	148	CR	10	2	618	0.2086	0.9308	−0.9308			1.05
2014_IALG	148	CR	11	3	618	0.7650	1.0664	0.1867	−1.2531		0.88
2014_IALG	149	MC	01	1	601	0.6983					1.17
2014_IALG	149	MC	02	1	601	−0.1417					1.06
2014_IALG	149	MC	03	1	601	0.5141					1.18
2014_IALG	149	MC	04	1	601	0.2970					0.91
2014_IALG	149	MC	05	1	601	−1.3438					1.05
2014_IALG	149	MC	06	1	601	0.0659					0.86
2014_IALG	149	MC	07	1	601	0.3055					0.94
2014_IALG	149	MC	08	1	601	−0.0066					1.00
2014_IALG	149	CR	09	2	601	0.3472	0.2225	−0.2225			0.89
2014_IALG	149	CR	10	3	601	1.8509	0.6154	1.1591	−1.7746		1.06
2014_IALG	149	CR	11	3	601	1.0134	0.2124	−0.1942	−0.0182		0.98
2014_IALG	150	MC	01	1	605	−1.4659					1.07
2014_IALG	150	MC	02	1	605	0.1580					0.97
2014_IALG	150	MC	03	1	605	−0.3812					0.98
2014_IALG	150	MC	04	1	605	0.8248					1.08
2014_IALG	150	MC	05	1	605	0.2746					1.03
2014_IALG	150	MC	06	1	605	0.1828					0.96
2014_IALG	150	MC	07	1	605	−0.9882					0.92
2014_IALG	150	MC	08	1	605	−0.3812					0.95
2014_IALG	150	CR	09	3	605	1.9255	0.5687	−1.2057	0.6370		0.96
2014_IALG	150	CR	10	4	605	1.0233	1.8302	−0.9050	−0.6877	−0.2375	1.14
2014_IALG	150	CR	11	2	605	0.8804	0.4706	−0.4706			0.93
2014_IALG	151	MC	01	1	593	0.1747					1.00

Test	Form	Type	Item	Max	N-Count	RID	S1	S2	S3	S4	INFIT
2014_IALG	151	MC	02	1	593	−0.3946					0.94
2014_IALG	151	MC	03	1	593	−0.3442					1.01
2014_IALG	151	MC	04	1	593	0.9867					1.23
2014_IALG	151	MC	05	1	593	−0.1254					1.04
2014_IALG	151	MC	06	1	593	−0.3694					0.88
2014_IALG	151	MC	07	1	593	−0.9424					0.99
2014_IALG	151	MC	08	1	593	0.5075					0.91
2014_IALG	151	CR	09	2	593	0.3208	−0.1056	0.1056			0.96
2014_IALG	151	CR	10	3	593	1.1653	0.5546	−0.4457	−0.1089		0.98
2014_IALG	151	CR	11	4	593	0.9263	−0.5377	−0.8186	0.7161	0.6402	1.10
2014_IALG	152	MC	01	1	596	−0.1132					0.91
2014_IALG	152	MC	02	1	596	−0.0634					0.93
2014_IALG	152	MC	03	1	596	1.5777					1.08
2014_IALG	152	MC	04	1	596	1.0154					1.02
2014_IALG	152	MC	05	1	596	0.1905					0.97
2014_IALG	152	MC	06	1	596	−0.5967					0.98
2014_IALG	152	MC	07	1	596	−0.7537					1.00
2014_IALG	152	MC	08	1	596	−0.8458					1.02
2014_IALG	152	CR	09	2	596	−0.6698	1.0704	−1.0704			0.94
2014_IALG	152	CR	10	3	596	−0.3216	0.1088	−0.4083	0.2995		1.14
2014_IALG	152	CR	11	4	596	1.4140	2.1668	−1.7027	0.4326	−0.8968	1.06
2014_IALG	153	MC	01	1	584	−0.6845					0.94
2014_IALG	153	MC	02	1	584	0.1728					1.09
2014_IALG	153	MC	03	1	584	−0.4964					1.05
2014_IALG	153	MC	04	1	584	−0.2134					1.07
2014_IALG	153	MC	05	1	584	−0.6928					0.97
2014_IALG	153	MC	06	1	584	1.0808					0.83
2014_IALG	153	MC	07	1	584	0.7969					1.01
2014_IALG	153	MC	08	1	584	0.1309					1.11
2014_IALG	153	CR	09	3	584	0.1468	0.5619	0.3263	−0.8881		0.88
2014_IALG	153	CR	10	4	584	0.0122	2.3309	−2.6642	0.3889	−0.0556	0.92
2014_IALG	153	CR	11	2	584	1.3001	0.7397	−0.7397			1.11
2014_IALG	154	MC	01	1	579	−0.2304					0.99
2014_IALG	154	MC	02	1	579	−0.0266					0.97
2014_IALG	154	MC	03	1	579	0.2928					0.96
2014_IALG	154	MC	04	1	579	−0.1492					1.01
2014_IALG	154	MC	05	1	579	0.7933					1.35
2014_IALG	154	MC	06	1	579	0.3891					1.03
2014_IALG	154	MC	07	1	579	−1.1467					0.93
2014_IALG	154	MC	08	1	579	0.6175					0.94

Test	Form	Type	Item	Max	N-Count	RID	S1	S2	S3	S4	INFIT
2014_IALG	154	CR	09	4	579	0.4380	0.5148	0.3232	0.2545	−1.0925	0.79
2014_IALG	154	CR	10	.							
2014_IALG	154	CR	11	3	579	1.7286	0.5448	−1.1523	0.6075		0.90
2014_IALG	155	MC	01	1	589	−1.6259					0.92
2014_IALG	155	MC	02	1	589	0.3227					1.09
2014_IALG	155	MC	03	1	589	0.2150					0.97
2014_IALG	155	MC	04	1	589	0.0568					0.97
2014_IALG	155	MC	05	1	589	0.4606					0.98
2014_IALG	155	MC	06	1	589	−0.7856					0.96
2014_IALG	155	MC	07	1	589	1.2880					1.16
2014_IALG	155	MC	08	1	589	−0.7417					1.02
2014_IALG	155	CR	09	3	589	1.7033	1.1521	−0.9751	−0.1770		0.91
2014_IALG	155	CR	10	4	589	1.1974	1.5170	0.4268	1.0775	−3.0213	0.84
2014_IALG	155	CR	11	2	589	0.7104	−0.3412	0.3412			1.08
2014_IALG	156	MC	01	1	576	0.4849					0.95
2014_IALG	156	MC	02	1	576	−0.0383					1.06
2014_IALG	156	MC	03	1	576	−0.4013					0.91
2014_IALG	156	MC	04	1	576	−1.5566					0.92
2014_IALG	156	MC	05	1	576	−0.0991					1.32
2014_IALG	156	MC	06	1	576	0.7605					0.96
2014_IALG	156	MC	07	1	576	−0.9685					1.01
2014_IALG	156	MC	08	1	576	0.8862					0.95
2014_IALG	156	CR	09	4	576	0.1891	1.2543	−0.5833	0.1239	−0.7950	0.74
2014_IALG	156	CR	10	3	576	1.2993	1.1731	0.6502	−1.8233		0.83
2014_IALG	156	CR	11	2	576	0.2083	−0.3513	0.3513			1.16
2014_IALG	157	MC	01	1	575	0.0963					1.06
2014_IALG	157	MC	02	1	575	−0.0233					1.07
2014_IALG	157	MC	03	1	575	1.2001					1.01
2014_IALG	157	MC	04	1	575	0.0448					0.93
2014_IALG	157	MC	05	1	575	2.4390					1.01
2014_IALG	157	MC	06	1	575	−0.4989					1.13
2014_IALG	157	MC	07	1	575	0.0192					0.87
2014_IALG	157	MC	08	1	575	−0.0908					1.05
2014_IALG	157	CR	09	2	575	−0.8924	1.0445	−1.0445			0.93
2014_IALG	157	CR	10	3	575	−0.4299	0.9293	−0.7541	−0.1752		0.94
2014_IALG	157	CR	11	4	575	0.6615	1.0205	0.1300	0.7330	−1.8836	0.84

Appendix E: DIF Statistics

The first four columns from the left contain the test name, form ID, item type, and item sequence number within the form. The next three columns contain the Mantel-Haenszel DIF statistical values (note that the MH Delta statistic cannot be calculated for CR items). The final two columns will only have values if the item displays possible moderate or severe DIF; if so, the degree of DIF (B/BB = moderate; C/CC = severe) and the favored group will be shown. Items without statistics are DNS (Do Not Score) status items.

Test	Form	Type	Item	MH Delta	MH Chi-Sq	Effect Size	DIF Category	Favored Group
2014_IALG	141	MC	01	−0.32	0.40	−0.05		
2014_IALG	141	MC	02	−1.00	3.06	−0.17		
2014_IALG	141	MC	03	−0.01	0.00	0.00		
2014_IALG	141	MC	04	0.12	0.05	0.01		
2014_IALG	141	MC	05	−0.58	1.70	−0.08		
2014_IALG	141	MC	06	0.79	2.43	0.10		
2014_IALG	141	MC	07	−1.31	7.75	−0.22	B	M
2014_IALG	141	MC	08	−0.03	0.00	−0.01		
2014_IALG	141	CR	09		0.39	−0.04		
2014_IALG	141	CR	10		3.43	0.11		
2014_IALG	141	CR	11		1.45	0.08		
2014_IALG	142	MC	01	−0.44	0.82	−0.05		
2014_IALG	142	MC	02	0.22	0.19	0.06		
2014_IALG	142	MC	03	−0.41	0.85	−0.03		
2014_IALG	142	MC	04	0.34	0.57	0.11		
2014_IALG	142	MC	05	0.63	1.21	0.10		
2014_IALG	142	MC	06	0.68	1.76	0.09		
2014_IALG	142	MC	07	−0.08	0.03	0.00		
2014_IALG	142	MC	08	−0.70	2.30	−0.12		
2014_IALG	142	CR	09		0.85	0.11		
2014_IALG	142	CR	10		1.36	−0.07		
2014_IALG	142	CR	11		0.31	0.02		
2014_IALG	143	MC	01	−0.64	1.31	−0.03		
2014_IALG	143	MC	02	−1.11	4.95	−0.15	B	M
2014_IALG	143	MC	03	0.82	2.92	0.15		
2014_IALG	143	MC	04	−0.37	0.68	−0.01		
2014_IALG	143	MC	05	−0.10	0.05	0.00		
2014_IALG	143	MC	06	−1.08	5.78	−0.18	B	M
2014_IALG	143	MC	07	−0.25	0.31	−0.04		
2014_IALG	143	MC	08	1.02	4.61	0.18	B	F

Test	Form	Type	Item	MH Delta	MH Chi-Sq	Effect Size	DIF Category	Favored Group
2014_IALG	143	CR	09		0.04	0.00		
2014_IALG	143	CR	10		0.78	0.09		
2014_IALG	143	CR	11		3.72	0.19		
2014_IALG	144	MC	01	−0.79	2.48	−0.11		
2014_IALG	144	MC	02	−0.37	0.51	−0.07		
2014_IALG	144	MC	03	−0.65	1.97	−0.10		
2014_IALG	144	MC	04	0.42	0.86	0.07		
2014_IALG	144	MC	05	−1.17	5.28	−0.17	B	M
2014_IALG	144	MC	06	−0.61	1.19	−0.07		
2014_IALG	144	MC	07	1.22	5.81	0.18	B	F
2014_IALG	144	MC	08	0.82	3.10	0.13		
2014_IALG	144	CR	09		2.81	0.11		
2014_IALG	144	CR	10		0.26	−0.04		
2014_IALG	144	CR	11		0.46	−0.06		
2014_IALG	145	MC	01	−0.04	0.01	0.03		
2014_IALG	145	MC	02	0.16	0.14	0.03		
2014_IALG	145	MC	03	0.03	0.00	0.01		
2014_IALG	145	MC	04	0.06	0.02	0.05		
2014_IALG	145	MC	05	0.63	1.89	0.16		
2014_IALG	145	MC	06	0.16	0.07	0.01		
2014_IALG	145	MC	07	−0.06	0.02	−0.02		
2014_IALG	145	MC	08	−0.53	1.12	−0.06		
2014_IALG	145	CR	09		1.45	0.12		
2014_IALG	145	CR	10		0.20	0.06		
2014_IALG	145	CR	11		4.86	−0.10		
2014_IALG	146	MC	01	0.54	1.42	0.08		
2014_IALG	146	MC	02	0.61	1.95	0.11		
2014_IALG	146	MC	03	−0.20	0.20	−0.03		
2014_IALG	146	MC	04	−0.37	0.71	−0.08		
2014_IALG	146	MC	05	0.12	0.06	0.03		
2014_IALG	146	MC	06	−0.26	0.36	−0.04		
2014_IALG	146	MC	07	−0.21	0.23	−0.03		
2014_IALG	146	MC	08	−0.45	0.83	−0.07		
2014_IALG	146	CR	09		2.55	−0.09		
2014_IALG	146	CR	10		0.08	−0.01		
2014_IALG	146	CR	11		2.48	0.07		
2014_IALG	147	MC	01	0.21	0.26	0.04		
2014_IALG	147	MC	02	0.16	0.10	0.04		

Test	Form	Type	Item	MH Delta	MH Chi-Sq	Effect Size	DIF Category	Favored Group
2014_IALG	147	MC	03	0.92	4.47	0.17		
2014_IALG	147	MC	04	0.37	0.70	0.06		
2014_IALG	147	MC	05	−0.36	0.56	−0.05		
2014_IALG	147	MC	06	−0.29	0.32	−0.06		
2014_IALG	147	MC	07	−0.51	1.32	−0.10		
2014_IALG	147	MC	08	−0.34	0.54	−0.03		
2014_IALG	147	CR	09		0.56	−0.05		
2014_IALG	147	CR	10		1.48	0.09		
2014_IALG	147	CR	11		0.26	−0.03		
2014_IALG	148	MC	01	0.30	0.51	0.06		
2014_IALG	148	MC	02	0.55	1.59	0.10		
2014_IALG	148	MC	03	0.75	2.92	0.14		
2014_IALG	148	MC	04	0.80	3.48	0.13		
2014_IALG	148	MC	05	−0.49	0.98	−0.09		
2014_IALG	148	MC	06	0.01	0.00	0.02		
2014_IALG	148	MC	07	−0.35	0.61	−0.06		
2014_IALG	148	MC	08	−0.11	0.05	−0.02		
2014_IALG	148	CR	09		0.19	0.02		
2014_IALG	148	CR	10		13.13	−0.25	CC	M
2014_IALG	148	CR	11		0.32	0.04		
2014_IALG	149	MC	01	0.12	0.06	0.01		
2014_IALG	149	MC	02	0.38	0.73	0.06		
2014_IALG	149	MC	03	−0.30	0.44	0.02		
2014_IALG	149	MC	04	0.14	0.08	0.02		
2014_IALG	149	MC	05	−0.96	3.70	−0.15		
2014_IALG	149	MC	06	−0.20	0.16	−0.03		
2014_IALG	149	MC	07	−0.17	0.11	−0.05		
2014_IALG	149	MC	08	0.04	0.01	0.00		
2014_IALG	149	CR	09		2.32	0.09		
2014_IALG	149	CR	10		1.33	−0.05		
2014_IALG	149	CR	11		0.34	0.07		
2014_IALG	150	MC	01	−1.17	5.36	−0.14	B	M
2014_IALG	150	MC	02	0.44	0.93	0.14		
2014_IALG	150	MC	03	0.69	2.26	0.15		
2014_IALG	150	MC	04	−0.65	1.91	−0.13		
2014_IALG	150	MC	05	0.07	0.02	0.07		
2014_IALG	150	MC	06	−0.11	0.06	0.02		
2014_IALG	150	MC	07	0.69	1.95	0.15		

Test	Form	Type	Item	MH Delta	MH Chi-Sq	Effect Size	DIF Category	Favored Group
2014_IALG	150	MC	08	−0.70	2.37	−0.07		
2014_IALG	150	CR	09		0.12	0.06		
2014_IALG	150	CR	10		0.00	0.08		
2014_IALG	150	CR	11		1.90	0.14		
2014_IALG	151	MC	01	1.12	5.70	0.18	B	F
2014_IALG	151	MC	02	−0.61	1.64	−0.09		
2014_IALG	151	MC	03	0.84	3.47	0.15		
2014_IALG	151	MC	04	−0.56	1.37	−0.12		
2014_IALG	151	MC	05	0.35	0.61	0.07		
2014_IALG	151	MC	06	−0.26	0.27	−0.05		
2014_IALG	151	MC	07	−1.05	5.02	−0.16	B	M
2014_IALG	151	MC	08	−0.97	3.61	−0.14		
2014_IALG	151	CR	09		1.71	−0.09		
2014_IALG	151	CR	10		9.66	0.20	BB	F
2014_IALG	151	CR	11		0.29	−0.03		
2014_IALG	152	MC	01	0.09	0.03	0.02		
2014_IALG	152	MC	02	−0.93	3.82	−0.14		
2014_IALG	152	MC	03	−0.65	1.31	−0.07		
2014_IALG	152	MC	04	0.45	0.76	0.06		
2014_IALG	152	MC	05	0.60	1.65	0.08		
2014_IALG	152	MC	06	−0.10	0.05	−0.01		
2014_IALG	152	MC	07	0.33	0.48	0.05		
2014_IALG	152	MC	08	0.62	1.83	0.12		
2014_IALG	152	CR	09		1.56	−0.08		
2014_IALG	152	CR	10		0.77	0.05		
2014_IALG	152	CR	11		0.53	−0.04		
2014_IALG	153	MC	01	−0.64	1.80	−0.10		
2014_IALG	153	MC	02	0.18	0.16	0.03		
2014_IALG	153	MC	03	−0.11	0.06	−0.03		
2014_IALG	153	MC	04	−0.31	0.53	−0.08		
2014_IALG	153	MC	05	0.19	0.16	0.02		
2014_IALG	153	MC	06	0.85	2.03	0.08		
2014_IALG	153	MC	07	−0.47	0.96	−0.08		
2014_IALG	153	MC	08	−0.08	0.03	−0.01		
2014_IALG	153	CR	09		0.08	0.03		
2014_IALG	153	CR	10		1.18	0.06		
2014_IALG	153	CR	11		1.56	−0.07		
2014_IALG	154	MC	01	−0.33	0.55	−0.05		

Test	Form	Type	Item	MH Delta	MH Chi-Sq	Effect Size	DIF Category	Favored Group
2014_IALG	154	MC	02	0.03	0.00	−0.01		
2014_IALG	154	MC	03	0.78	2.67	0.12		
2014_IALG	154	MC	04	0.07	0.02	0.00		
2014_IALG	154	MC	05	−0.73	2.34	−0.14		
2014_IALG	154	MC	06	−0.24	0.29	−0.06		
2014_IALG	154	MC	07	−0.48	0.97	−0.06		
2014_IALG	154	MC	08	−0.24	0.24	−0.03		
2014_IALG	154	CR	09		4.51	0.11		
2014_IALG	154	CR	10					
2014_IALG	154	CR	11		2.13	−0.09		
2014_IALG	155	MC	01	0.49	0.77	0.10		
2014_IALG	155	MC	02	−0.23	0.25	0.00		
2014_IALG	155	MC	03	0.31	0.42	0.06		
2014_IALG	155	MC	04	0.41	0.73	0.09		
2014_IALG	155	MC	05	0.16	0.10	0.05		
2014_IALG	155	MC	06	−0.78	2.62	−0.08		
2014_IALG	155	MC	07	−0.95	3.07	−0.12		
2014_IALG	155	MC	08	1.17	6.43	0.23	B	F
2014_IALG	155	CR	09		0.45	−0.04		
2014_IALG	155	CR	10		0.12	0.09		
2014_IALG	155	CR	11		0.91	−0.02		
2014_IALG	156	MC	01	−0.80	2.57	−0.12		
2014_IALG	156	MC	02	0.84	3.37	0.16		
2014_IALG	156	MC	03	0.43	0.77	0.09		
2014_IALG	156	MC	04	1.15	4.09	0.13	B	F
2014_IALG	156	MC	05	0.51	1.39	0.07		
2014_IALG	156	MC	06	−0.53	1.02	−0.09		
2014_IALG	156	MC	07	−1.20	5.83	−0.20	B	M
2014_IALG	156	MC	08	−1.76	11.05	−0.28	C	M
2014_IALG	156	CR	09		0.26	−0.02		
2014_IALG	156	CR	10		1.00	0.05		
2014_IALG	156	CR	11		1.54	0.11		
2014_IALG	157	MC	01	−0.24	0.30	−0.05		
2014_IALG	157	MC	02	0.19	0.18	0.04		
2014_IALG	157	MC	03	−1.11	4.08	−0.16	B	M
2014_IALG	157	MC	04	1.33	8.18	0.24	B	F
2014_IALG	157	MC	05	0.61	0.55	0.06		
2014_IALG	157	MC	06	0.02	0.00	0.00		

Test	Form	Type	Item	MH Delta	MH Chi-Sq	Effect Size	DIF Category	Favored Group
2014_IALG	157	MC	07	−0.09	0.04	−0.01		
2014_IALG	157	MC	08	−0.69	2.31	−0.13		
2014_IALG	157	CR	09		0.59	−0.05		
2014_IALG	157	CR	10		0.00	0.00		
2014_IALG	157	CR	11		0.84	0.04		

DIF category meanings: A/AA = negligible, B/BB = moderate, C/CC = severe.

Favored group meanings: F = Female, M = Male.

Appendix F: Operational Test Maps

January 2014

Pos	Item Type	Max Points	Weight	Standard	Key Idea	PI	Mean	Pt Bis	RID	INFIT
1	MC	1	2	Algebra		A.A.3	0.74	0.45	-1.5598	0.92
2	MC	1	2	Algebra		A.A.20	0.71	0.45	-1.5388	0.92
3	MC	1	2	Algebra		A.A.6	0.55	0.45	-0.3474	1.04
4	MC	1	2	Statistics and Probability		A.S.15	0.45	0.35	-0.1700	1.09
5	MC	1	2	Geometry		A.G.3	0.56	0.36	-0.7200	1.07
6	MC	1	2	Algebra		A.A.34	0.65	0.49	-1.0700	0.94
7	MC	1	2	Geometry		A.G.1	0.15	0.24	1.8668	1.09
8	MC	1	2	Statistics and Probability		A.S.6	0.61	0.39	-0.9084	1.03
9	MC	1	2	Algebra		A.A.37	0.53	0.40	-0.5984	1.02
10	MC	1	2	Algebra		A.A.10	0.58	0.37	-0.8149	1.03
11	MC	1	2	Statistics and Probability		A.S.17	0.38	0.27	0.1900	1.13
12	MC	1	2	Algebra		A.A.14	0.56	0.33	-0.7512	1.13
13	MC	1	2	Algebra		A.A.5	0.56	0.48	-0.6800	0.99
14	MC	1	2	Statistics and Probability		A.S.1	0.56	0.36	-0.6300	1.06
15	MC	1	2	Statistics and Probability		A.S.21	0.57	0.25	-0.7668	1.14
16	MC	1	2	Algebra		A.A.41	0.54	0.36	-0.5268	1.01
17	MC	1	2	Algebra		A.A.45	0.52	0.49	-0.4736	0.92
18	MC	1	2	Algebra		A.A.24	0.59	0.37	-0.8738	1.05
19	MC	1	2	Measurement		A.M.1	0.47	0.27	-0.2400	1.10
20	MC	1	2	Algebra		A.A.17	0.45	0.55	-0.2000	0.86
21	MC	1	2	Number Sense and Operations		A.N.6	0.43	0.41	-0.1852	1.01
22	MC	1	2	Geometry		A.G.6	0.45	0.34	-0.0904	1.04
23	MC	1	2	Geometry		A.G.4	0.45	0.38	-0.2258	1.05
24	MC	1	2	Algebra		A.A.16	0.43	0.46	-0.0600	0.95
25	MC	1	2	Algebra		A.A.23	0.42	0.48	-0.0688	0.97
26	MC	1	2	Algebra		A.A.30	0.44	0.49	-0.0800	1.02
27	MC	1	2	Algebra		A.A.27	0.34	0.35	0.3128	1.03
28	MC	1	2	Number Sense and Operations		A.N.1	0.31	0.41	0.5734	0.99
29	MC	1	2	Algebra		A.A.13	0.35	0.43	0.3584	0.98
30	MC	1	2	Algebra		A.A.1	0.18	0.32	1.2400	0.98
31	CR	2	1	Number Sense and Operations		A.N.3	0.44	0.48	0.7600	0.89
32	CR	2	1	Statistics and Probability		A.S.9	0.26	0.51	1.9968	0.96
33	CR	2	1	Algebra		A.A.9	0.43	0.50	0.8969	0.96

Pos	Item Type	Max Points	Weight	Standard	Key Idea	PI	Mean	Pt Bis	RID	INFIT
34	CR	3	1	Geometry		A.G.5	0.46	0.54	1.1000	0.91
35	CR	3	1	Measurement		A.M.3	0.06	0.25	2.7800	0.91
36	CR	3	1	Algebra		A.A.44	0.45	0.55	1.0800	1.00
37	CR	4	1	Geometry		A.G.9	1.12	0.71	0.3949	0.92
38	CR	4	1	Algebra		A.A.26	0.74	0.70	0.6429	0.84
39	CR	4	1	Statistics and Probability		A.S.19	2.22	0.72	-0.4700	0.88

June 2014

Pos	Item Type	Max Points	Weight	Standard	Key Idea	PI	Mean	Pt Bis	RID	INFIT
1	MC	1	2	Algebra		A.A.12	0.79	0.35	-1.8199	0.98
2	MC	1	2	Statistics and Probability		A.S.1	0.51	0.43	-0.1580	1.04
3	MC	1	2	Measurement		A.M.1	0.68	0.42	-1.2583	1.00
4	MC	1	2	Geometry		A.G.8	0.61	0.37	-0.9264	1.06
5	MC	1	2	Number Sense and Operations		A.N.1	0.77	0.42	-1.8862	0.94
6	MC	1	2	Algebra		A.A.24	0.62	0.50	-0.8284	0.90
7	MC	1	2	Statistics and Probability		A.S.15	0.84	0.29	-2.1163	1.04
8	MC	1	2	Algebra		A.A.3	0.69	0.44	-1.0264	0.95
9	MC	1	2	Algebra		A.A.10	0.56	0.44	-0.6253	0.94
10	MC	1	2	Algebra		A.A.33	0.55	0.41	-0.6079	1.05
11	MC	1	2	Algebra		A.A.29	0.52	0.39	-0.4298	1.00
12	MC	1	2	Number Sense and Operations		A.N.6	0.57	0.47	-0.4603	1.03
13	MC	1	2	Geometry		A.G.3	0.47	0.39	-0.2085	1.09
14	MC	1	2	Algebra		A.A.13	0.39	0.48	0.4298	0.96
15	MC	1	2	Algebra		A.A.45	0.47	0.45	-0.1919	0.94
16	MC	1	2	Algebra		A.A.36	0.45	0.54	-0.1026	0.90
17	MC	1	2	Algebra		A.A.42	0.45	0.47	-0.0895	0.98
18	MC	1	2	Algebra		A.A.4	0.41	0.45	-0.0700	0.99
19	MC	1	2	Algebra		A.A.34	0.53	0.42	-0.2384	1.01
20	MC	1	2	Geometry		A.G.10	0.32	0.34	0.3769	1.05
21	MC	1	2	Algebra		A.A.20	0.32	0.43	0.3916	0.96
22	MC	1	2	Algebra		A.A.8	0.40	0.42	0.1100	0.99
23	MC	1	2	Geometry		A.G.4	0.43	0.42	-0.0231	1.04
24	MC	1	2	Algebra		A.A.17	0.19	0.22	1.2124	1.12
25	MC	1	2	Algebra		A.A.22	0.84	0.37	-1.9966	0.98
26	MC	1	2	Algebra		A.A.31	0.35	0.36	0.3834	1.12
27	MC	1	2	Statistics and Probability		A.S.14	0.60	0.27	-0.9200	1.20
28	MC	1	2	Statistics and Probability		A.S.19	0.61	0.50	-0.9334	0.91
29	MC	1	2	Algebra		A.A.15	0.32	0.44	0.5298	0.99
30	MC	1	2	Number Sense and Operations		A.N.4	0.30	0.38	0.5152	1.02
31	CR	2	1	Geometry		AA.1	0.16	0.48	1.8343	0.88
32	CR	2	1	Geometry		A.G.1	0.22	0.47	1.5032	0.93
33	CR	2	1	Statistics and Probability		A.S.23	0.28	0.48	1.3700	0.89
34	CR	3	1	Algebra		A.A.11	0.55	0.67	0.8531	0.85
35	CR	3	1	Measurement		A.M.3	0.86	0.68	0.7288	0.97
36	CR	3	1	Number Sense and Operations		A.N.3	0.48	0.57	1.4628	1.04

Pos	Item Type	Max Points	Weight	Standard	Key Idea	PI	Mean	Pt Bis	RID	INFIT
37	CR	4	1	Algebra		A.A.7	0.69	0.71	1.0857	0.88
38	CR	4	1	Geometry		A.G.7	0.80	0.75	0.7390	0.77
39	CR	4	1	Statistics and Probability		A.S.5	1.05	0.69	0.3866	0.99

August 2014

Pos	Item Type	Max Points	Weight	Standard	Key Idea	PI	Mean	Pt Bis	RID	INFIT
1	MC	1	2	Algebra		A.A.12	0.72	0.46	-1.5374	0.92
2	MC	1	2	Number Sense and Operations		A.N.6	0.67	0.53	-1.3200	0.94
3	MC	1	2	Algebra		A.A.19	0.72	0.49	-1.3213	0.87
4	MC	1	2	Algebra		A.A.35	0.60	0.47	-0.9573	0.92
5	MC	1	2	Geometry		A.G.10	0.63	0.45	-0.9900	0.96
6	MC	1	2	Statistics and Probability		A.S.3	0.53	0.34	-0.6189	1.14
7	MC	1	2	Statistics and Probability		A.S.12	0.62	0.38	-0.8566	1.05
8	MC	1	2	Algebra		A.A.31	0.80	0.40	-1.8693	0.97
9	MC	1	2	Algebra		A.A.17	0.59	0.47	-0.7091	0.95
10	MC	1	2	Algebra		A.A.4	0.59	0.40	-0.6840	0.99
11	MC	1	2	Algebra		A.A.33	0.57	0.36	-0.6052	1.03
12	MC	1	2	Statistics and Probability		A.S.1	0.53	0.42	-0.4272	0.96
13	MC	1	2	Statistics and Probability		A.S.19	0.57	0.37	-0.5618	1.00
14	MC	1	2	Geometry		A.G.5	0.50	0.39	-0.4400	1.02
15	MC	1	2	Measurement		A.M.2	0.50	0.47	-0.2759	0.94
16	MC	1	2	Algebra		A.A.25	0.41	0.36	-0.0055	1.09
17	MC	1	2	Algebra		A.A.15	0.47	0.46	-0.1131	0.96
18	MC	1	2	Algebra		A.A.42	0.46	0.41	-0.1087	0.99
19	MC	1	2	Number Sense and Operations		A.N.1	0.84	0.39	-2.4289	0.90
20	MC	1	2	Algebra		A.A.28	0.45	0.48	-0.0470	0.94
21	MC	1	2	Statistics and Probability		A.S.4	0.45	0.44	-0.0246	0.97
22	MC	1	2	Algebra		A.A.9	0.42	0.21	0.1228	1.16
23	MC	1	2	Algebra		A.A.36	0.41	0.41	0.1264	1.01
24	MC	1	2	Algebra		A.A.5	0.41	0.39	0.1581	1.02
25	MC	1	2	Geometry		AA.4	0.41	0.43	0.1752	0.98
26	MC	1	2	Algebra		A.A.23	0.40	0.31	0.1533	1.10
27	MC	1	2	Algebra		A.A.38	0.39	0.35	0.2329	1.03
28	MC	1	2	Algebra		A.A.13	0.39	0.51	0.2376	0.91
29	MC	1	2	Algebra		A.A.26	0.34	0.31	0.3038	1.11
30	MC	1	2	Algebra		A.A.29	0.33	0.32	0.5273	1.09
31	CR	2	1	Statistics and Probability		A.S.5	1.03	0.57	-0.2964	1.01
32	CR	2	1	Geometry		A.G.1	0.15	0.40	1.8100	0.97
33	CR	2	1	Geometry		A.G.2	0.50	0.55	0.9085	0.94
34	CR	3	1	Algebra		A.A.44	0.55	0.64	0.7644	0.91
35	CR	3	1	Statistics and Probability		A.S.23	0.40	0.64	0.9425	0.80
36	CR	3	1	Number Sense and Operations		A.N.3	0.25	0.57	1.7689	0.85

Pos	Item Type	Max Points	Weight	Standard	Key Idea	PI	Mean	Pt Bis	RID	INFIT
37	CR	4	1	Geometry		A.G.7	0.66	0.70	0.9955	0.84
38	CR	4	1	Measurement		A.M.3	0.33	0.54	1.7621	1.03
39	CR	4	1	Algebra		A.A.11	0.67	0.58	0.8600	0.88

Appendix G: Scoring Tables

January 2014

Raw Score	Ability	Scale Score
0	−5.841	0.000
1	−4.623	4.592
2	−3.910	8.542
3	−3.485	12.226
4	−3.177	15.670
5	−2.934	18.923
6	−2.733	21.983
7	−2.559	24.867
8	−2.407	27.594
9	−2.270	30.163
10	−2.145	32.615
11	−2.031	34.931
12	−1.925	37.124
13	−1.827	39.214
14	−1.734	41.220
15	−1.646	43.134
16	−1.562	44.959
17	−1.483	46.716
18	−1.406	48.393
19	−1.332	50.007
20	−1.261	51.573
21	−1.192	53.085
22	−1.125	54.533

Raw Score	Ability	Scale Score
23	−1.059	55.927
24	−0.995	57.295
25	−0.932	58.601
26	−0.870	59.860
27	−0.809	61.084
28	−0.749	62.279
29	−0.689	63.430
30	−0.631	64.538
31	−0.573	65.605
32	−0.515	66.628
33	−0.458	67.620
34	−0.402	68.575
35	−0.346	69.482
36	−0.290	70.353
37	−0.235	71.185
38	−0.181	71.977
39	−0.126	72.742
40	−0.073	73.473
41	−0.019	74.156
42	0.034	74.805
43	0.086	75.425
44	0.138	76.015
45	0.190	76.581

Raw Score	Ability	Scale Score
46	0.241	77.112
47	0.292	77.616
48	0.343	78.098
49	0.393	78.553
50	0.444	78.992
51	0.494	79.417
52	0.544	79.822
53	0.594	80.214
54	0.644	80.595
55	0.695	80.970
56	0.746	81.345
57	0.798	81.705
58	0.850	82.068
59	0.903	82.429
60	0.957	82.792
61	1.012	83.161
62	1.068	83.542
63	1.126	83.924
64	1.186	84.317
65	1.248	84.731
66	1.312	85.161
67	1.378	85.614
68	1.447	86.089

Raw Score	Ability	Scale Score
69	1.520	86.580
70	1.596	87.105
71	1.676	87.662
72	1.761	88.244
73	1.851	88.859
74	1.947	89.503
75	2.050	90.181
76	2.160	90.887
77	2.279	91.620
78	2.407	92.371
79	2.547	93.134
80	2.699	93.905
81	2.869	94.687
82	3.062	95.476
83	3.289	96.278
84	3.574	97.109
85	3.968	97.982
86	4.644	98.974
87	5.834	100.000

June 2014

Raw Score	Ability	Scale Score
0	−6.095	0.000
1	−4.869	3.457
2	−4.146	6.799
3	−3.709	10.026
4	−3.391	13.140
5	−3.137	16.141
6	−2.924	19.061
7	−2.740	21.876
8	−2.575	24.589
9	−2.427	27.220
10	−2.291	29.754
11	−2.165	32.224
12	−2.047	34.602
13	−1.937	36.891
14	−1.832	39.101
15	−1.732	41.251
16	−1.637	43.325
17	−1.546	45.321
18	−1.458	47.259
19	−1.373	49.106
20	−1.291	50.908
21	−1.212	52.651
22	−1.135	54.317
23	−1.060	55.911
24	−0.987	57.464
25	−0.915	58.937
26	−0.846	60.348
27	−0.778	61.707
28	−0.711	63.016
29	−0.646	64.258
30	−0.582	65.438
31	−0.519	66.556
32	−0.458	67.624
33	−0.398	68.640
34	−0.339	69.594
35	−0.281	70.498
36	−0.224	71.349
37	−0.168	72.154
38	−0.113	72.924
39	−0.059	73.647
40	−0.006	74.317
41	0.046	74.955
42	0.098	75.556
43	0.148	76.128
44	0.199	76.675
45	0.248	77.183
46	0.298	77.668
47	0.346	78.128
48	0.395	78.564
49	0.443	78.985
50	0.491	79.391
51	0.538	79.778
52	0.586	80.151
53	0.633	80.514
54	0.681	80.864
55	0.729	81.221
56	0.776	81.556
57	0.824	81.891
58	0.872	82.223
59	0.921	82.552
60	0.970	82.880
61	1.020	83.213
62	1.070	83.551
63	1.121	83.887
64	1.173	84.228
65	1.226	84.585
66	1.280	84.949
67	1.336	85.331
68	1.395	85.727
69	1.455	86.141
70	1.518	86.566
71	1.584	87.020
72	1.653	87.503
73	1.727	88.011
74	1.806	88.549
75	1.890	89.120
76	1.981	89.730
77	2.081	90.380
78	2.190	91.073
79	2.312	91.817
80	2.448	92.605
81	2.606	93.447
82	2.790	94.337
83	3.015	95.298
84	3.304	96.324
85	3.710	97.429
86	4.402	98.618
87	5.604	100.000

August 2014

Raw Score	Ability	Scale Score
0	−6.067	0.000
1	−4.841	3.588
2	−4.116	7.014
3	−3.680	10.314
4	−3.362	13.484
5	−3.109	16.529
6	−2.897	19.480
7	−2.713	22.311
8	−2.550	25.029
9	−2.403	27.654
10	−2.269	30.175
11	−2.145	32.621
12	−2.030	34.965
13	−1.921	37.216
14	−1.819	39.386
15	−1.721	41.489
16	−1.628	43.514
17	−1.540	45.457
18	−1.454	47.345
19	−1.372	49.140
20	−1.292	50.891
21	−1.215	52.585
22	−1.140	54.205
23	−1.067	55.756
24	−0.996	57.271
25	−0.926	58.714
26	−0.858	60.096
27	−0.792	61.430
28	−0.726	62.727
29	−0.662	63.957
30	−0.599	65.134
31	−0.537	66.257
32	−0.475	67.325
33	−0.415	68.361
34	−0.355	69.332
35	−0.297	70.257
36	−0.239	71.135
37	−0.181	71.966
38	−0.125	72.763
39	−0.069	73.518
40	−0.014	74.219
41	0.040	74.884
42	0.094	75.513
43	0.147	76.109
44	0.199	76.679
45	0.251	77.206
46	0.302	77.708
47	0.352	78.181
48	0.402	78.627
49	0.451	79.057
50	0.500	79.468
51	0.549	79.859
52	0.597	80.234
53	0.645	80.598
54	0.693	80.952
55	0.741	81.307
56	0.789	81.642
57	0.837	81.979
58	0.885	82.312
59	0.935	82.643
60	0.984	82.974
61	1.035	83.315
62	1.086	83.658
63	1.138	84.003
64	1.192	84.359
65	1.247	84.729
66	1.304	85.111
67	1.363	85.512
68	1.424	85.929
69	1.487	86.362
70	1.553	86.807
71	1.622	87.286
72	1.694	87.786
73	1.770	88.306
74	1.850	88.852
75	1.935	89.421
76	2.026	90.023
77	2.123	90.650
78	2.228	91.308
79	2.343	92.004
80	2.471	92.728
81	2.616	93.497
82	2.785	94.313
83	2.989	95.199
84	3.252	96.161
85	3.625	97.231
86	4.276	98.434
87	5.444	100.000