

**NEW YORK STATE  
COMPONENT RETEST**

**MATHEMATICS A  
COMPONENT 5  
MODULE 1**

**MONDAY, MAY 12, 2003**

**SCORING KEY  
AND  
RATING GUIDE**

**Multiple Choice Key**

1	1
2	2
3	3
4	3
5	4
6	2

**Math A Component Retest**  
**May 2003**  
**Component 5, Module 1**

**Key to Multiple-Choice Questions**

(1)	1
(2)	2
(3)	3
(4)	3
(5)	4
(6)	2

**Rubric**

(7)

[ 4 ] Mean = 20, median = 16.5, and mode = 31, and appropriate work is shown.

[ 3 ] Mean = 20, median = 16.5, and mode = 31, but no work is shown for the mean, but the data are ordered for the median.

*or*

[ 3 ] The mean and median are correct, and appropriate work is shown, but the mode is incorrect.

*or*

[ 3 ] Appropriate work is shown, and the mode is correct, but one computational error is made when finding the mean or median.

*or*

[ 3 ] 20, 16.5, and 31, and appropriate work is shown, but the values are not identified as the mean, median, or mode, or they are identified incorrectly.

[ 2 ] The median and mode are found correctly, and appropriate work is shown, but the mean is not found or more than one computational error is made in finding the mean.

*or*

[ 2 ] The mean is found correctly, but the median and mode are not found or are found incorrectly.

[ 1 ] Only the median or mode is found correctly, but appropriate work is shown.

*or*

[ 1 ] Mean = 20, median = 16.5, and mode = 31, but no work is shown.

[ 0 ] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

## Part II

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

- 7 In eight consecutive football games, the Buffalo Bills scored the following number of points: 31, 16, 10, 31, 16, 17, 8, 31. Determine the mean, median, and mode for this set of scores.

$$\begin{aligned} \text{mean} &= 20 \\ \text{median} &= 16.5 \\ \text{mode} &= 31 \end{aligned}$$

$$8 + 10 + 16 + 16 + 17 + 31 + 31 + 31 = \frac{160}{8} = 20$$
$$\frac{33}{2} = 16.5$$

Part II

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

- 7 In eight consecutive football games, the Buffalo Bills scored the following number of points: ~~31, 16, 10, 31, 17, 31~~ Determine the mean, median, and mode for this set of scores.

$\rightarrow$  mean = 20  
 $\rightarrow$  median = 16.5  
 $\rightarrow$  mode = 31, 16

8, 10, 16, (6+17) 31, 31, 31

$16 + 17 = 33$

$33 / 2 = 16.5$

$$\begin{array}{r} 31 \\ 16 \\ 10 \\ 31 \\ 16 \\ 17 \\ 8 \\ + 31 \\ \hline 160 \end{array}$$

$160 \div 8 = 20$

Part II

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

- 7 In eight consecutive football games, the Buffalo Bills scored the following number of points: 31, ~~16~~, ~~16~~, 31, ~~16~~, ~~17~~, ~~8~~, 31. Determine the mean, median, and mode for this set of scores.

Handwritten work for the mean and mode:

$$\begin{array}{r} 31 \\ + 31 \\ \hline 8 \overline{) 160} \end{array}$$

20 = mean

31 = mode

$$\begin{array}{r} 31 \\ 8 \\ \hline 23 \end{array}$$

Handwritten notes: 16 = median

Handwritten work for the median:

20 = mean

17 = median

16 = mode

Part II

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

- 7 In eight consecutive football games, the Buffalo Bills scored the following number of points: 31, 16, ~~10~~, 31, 16, 17, ~~8~~, 31. Determine the mean, median, and mode for this set of scores.

mean - ~~8, 10, 16, 17, 31, 31, 31~~

median -  $16\frac{1}{2}$

mode  $\frac{160}{8} = 20$

Part II

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

- 7 In eight consecutive football games, the Buffalo Bills scored the following number of points: ~~31, 10, 10, 31, 15, 17, 9, 31~~. Determine the mean, median, and mode for this set of scores.

~~40, 10, 16, 16, 17, 31, 31, 31~~

13.5 median

10 11 12 13 14 15 16 17

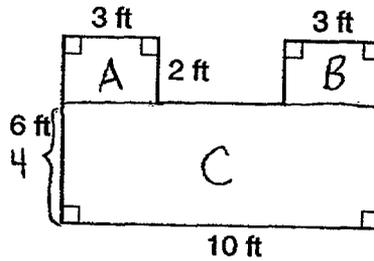
### Rubric

(8)

- [ 4 ] \$117, and appropriate work is shown, such as  $2.25(4 \times 10 + 2 \times 3 + 2 \times 3)$ .
- [ 3 ] Appropriate work is shown, but one computational error is made.
- [ 2 ] The cost of tiling two of the three regions is calculated correctly.
- or*
- [ 2 ] Correct area is found and appropriate work is shown, but no cost is calculated.
- or*
- [ 2 ] Correct area is found, but no work is shown, but a correct cost is calculated.
- or*
- [ 2 ] The area is found incorrectly, such as by using an incorrect area formula, but an appropriate cost is calculated.
- or*
- [ 2 ] Appropriate work is shown, but more than one computational error is made.
- [ 1 ] The perimeter is found instead of the area, but it is correctly multiplied by \$2.25.
- or*
- [ 1 ] \$117, but no work is shown.
- [ 0 ] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- 8 Sammy is planning to tile the floor shown in the accompanying diagram. If each tile measures 1 foot by 1 foot and costs \$2.25, what will be the cost of tiling the floor?

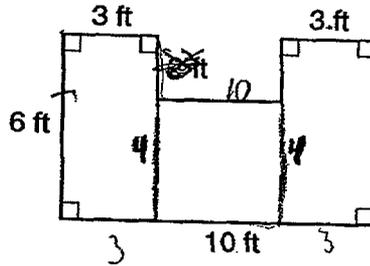
$$\begin{aligned} \text{Area}_A &= 3(2) = 6 \text{ ft}^2 \\ \text{Area}_B &= 3(2) = 6 \text{ ft}^2 \\ \text{Area}_C &= 4(10) = 40 \text{ ft}^2 \\ \hline &52 \text{ ft}^2 \end{aligned}$$



$$\begin{array}{r} 52 \\ \times 2.25 \\ \hline 117 \end{array}$$

\$117

- 8 Sammy is planning to tile the floor shown in the accompanying diagram. If each tile measures 1 foot by 1 foot and costs \$2.25, what will be the cost of tiling the floor?



$$A = Lw$$

$$A = 3(6)$$

$$A = 18$$

$$A = Lw$$

$$A = 3(6)$$

$$A = 18$$

$$A = Lw$$

$$A = 10(4)$$

$$A = 40$$

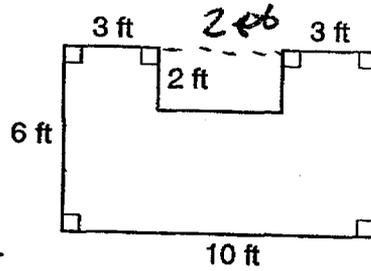
$$\begin{array}{r} 40 \\ + 18 \\ + 18 \\ \hline 76 \end{array}$$

$$\begin{array}{r} 76 \\ \times 2.25 \\ \hline 171 \end{array}$$

ans

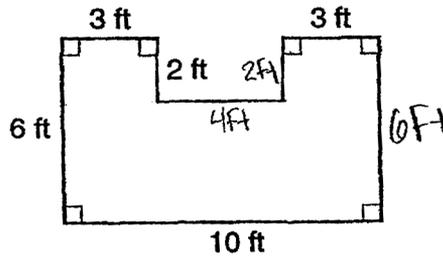
- 8 Sammy is planning to tile the floor shown in the accompanying diagram. If each tile measures 1 foot by 1 foot and costs \$2.25, what will be the cost of tiling the floor?

$$A = LW$$
$$A = 10 \cdot 6$$



$$60 \times 2.25$$
$$\$ 135.00$$

- 8 Sammy is planning to tile the floor shown in the accompanying diagram. If each tile measures 1 foot by 1 foot and costs \$2.25, what will be the cost of tiling the floor?

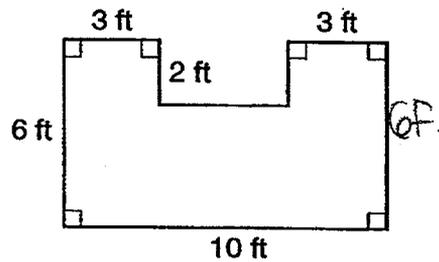


$$\begin{array}{r}
 10 \\
 6 \\
 6 \\
 3 \\
 2 \\
 4 \\
 2 \\
 + 3 \\
 \hline
 36
 \end{array}$$

$$\begin{array}{r}
 \$ 2.25 \\
 \times 36 \\
 \hline
 \$ 81.00
 \end{array}$$

Cost = \$81.00

- 8 Sammy is planning to tile the floor shown in the accompanying diagram. If each tile measures 1 foot by 1 foot and costs \$2.25, what will be the cost of tiling the floor?



Circled ones  
aren't  
answers!

$$6\text{ ft} + 6\text{ ft} = 12\text{ ft}$$

$$12\text{ ft} \cdot 2.25 = 27$$

$$3\text{ ft} + 3\text{ ft} = 6\text{ ft}$$

$$6\text{ ft} \cdot 2.25 = 13.50$$

$$2\text{ ft} \cdot 2.25 = 4.50$$

$$10\text{ ft} \cdot 2.25 = 22.5$$

27.00

13.50

4.50

± 22.50

\$67.50 is  
the cost  
of tiling  
the floor.

## Rubric

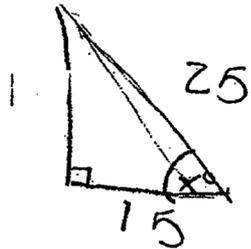
(9)

- [ 4 ]  $53^\circ$  and 20, and appropriate work is shown, such as  $\cos A = \frac{15}{25}$  and the 3–4–5 Pythagorean triple is stated.
- [ 3 ] Appropriate work is shown, but one computational error is made.  
*or*
- [ 3 ] The height is found correctly and a correct equation is written to find the angle, but no further correct work is shown.
- [ 2 ] One conceptual error is made, but appropriate answers are found.  
*or*
- [ 2 ] Either the angle or the height is determined correctly, and appropriate work is shown.
- [ 1 ]  $53^\circ$  and 20, but no work is shown.
- [ 0 ]  $53^\circ$  *or* 20, but no work is shown.  
*or*
- [ 0 ] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- 9 A 25-foot wire stretches from the top of a vertical pole to a stake 15 feet from the base of the pole on level ground.

Find the angle that the wire makes with the ground to the *nearest degree*.

Find the height of the pole to the *nearest foot*.



$$\cos x = \frac{15}{25}$$

$$x = 53.1$$

$$a^2 + b^2 = c^2$$

$$a^2 + 15^2 = 25^2$$

$$a^2 + 225 = 625$$

$$a^2 = 400$$

$$a = \sqrt{400}$$

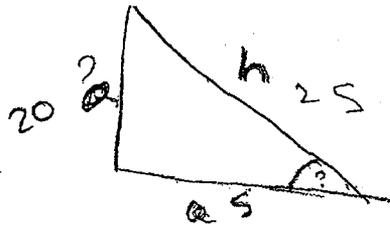
$$a = 20$$

The angle is  $53^\circ$ .  
The pole is 20 feet  
from the ground

- 9 A 25-foot wire stretches from the top of a vertical pole to a stake 15 feet from the base of the pole on level ground.

Find the angle that the wire makes with the ground to the *nearest degree*.

Find the height of the pole to the *nearest foot*.



Soh  
Cah  
Toa

$$\sin x = \frac{20}{25}$$

$$\sin x = 0.8$$

$$\sin x = 54$$

pole = 20ft

$$15^2 + x^2 = 25^2$$

$$225 + x^2 = 625$$

$$x^2 = 400$$

$$x = 20$$

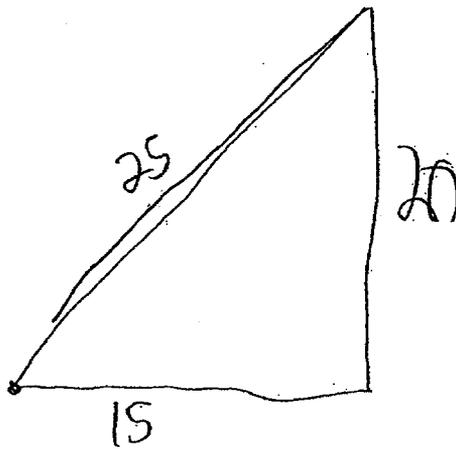
nearest degree = 54°

- 9 A 25-foot wire stretches from the top of a vertical pole to a stake 15 feet from the base of the pole on level ground.

Find the angle that the wire makes with the ground to the *nearest degree*.

Find the height of the pole to the *nearest foot*.

20ft



$$A^2 + b^2 = C^2$$

$$15^2 + b^2 = 25^2$$

$$\begin{array}{r} 225 + b^2 = 625 \\ -225 \\ \hline \end{array}$$

$$b^2 = 400$$

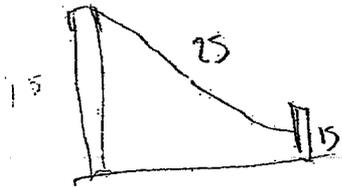
$$\sqrt{400}$$

$$b = 20$$

- 9 A 25-foot wire stretches from the top of a vertical pole to a stake 15 feet from the base of the pole on level ground.

Find the angle that the wire makes with the ground to the *nearest degree*.

Find the height of the pole to the *nearest foot*.



50ft

$$A^2 + b^2 = c^2$$

$$A^2 + 15^2 = 25^2$$

$$\begin{array}{r} A + 75 = 125 \\ - 75 \quad - 75 \\ \hline 50 \end{array}$$

$$\begin{array}{r} 75 \\ \times 15 \\ \hline 75 \end{array}$$